



# COMSOL ® Design Tool: Simulations of Optical Components Week 6: Waveguides and Propagation 3 – S Parameters

Xinzhi Zhang & Guillaume Zajac

# Content

- **Revision wave propagation**

- Waveguide
- Confinement
- Modes

- **S-parameters**

- Theory

- **Projects**

- Outline
- Short overview projects

Theory

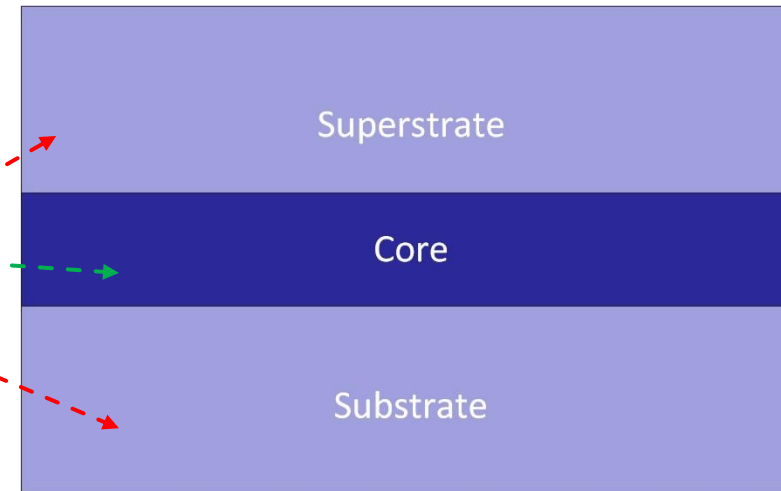
- **COMSOL examples**

- Taper
- Waveguide bend

Tutorial

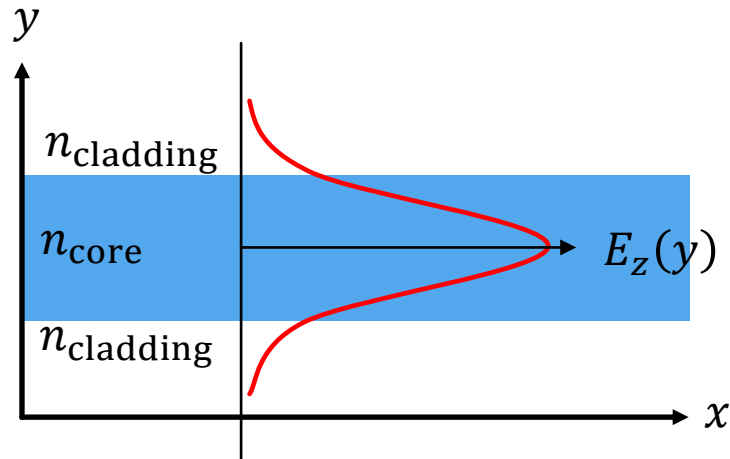
# Revision Wave Propagation

- Dielectric slab waveguide
- What we want
  - Propagation in core
  - Decay (exponential) in sub/superstrate
  - High confinement
- What we don't want
  - Propagation in sub/superstrate
  - Low confinement (except in certain application - e.g. couplers)

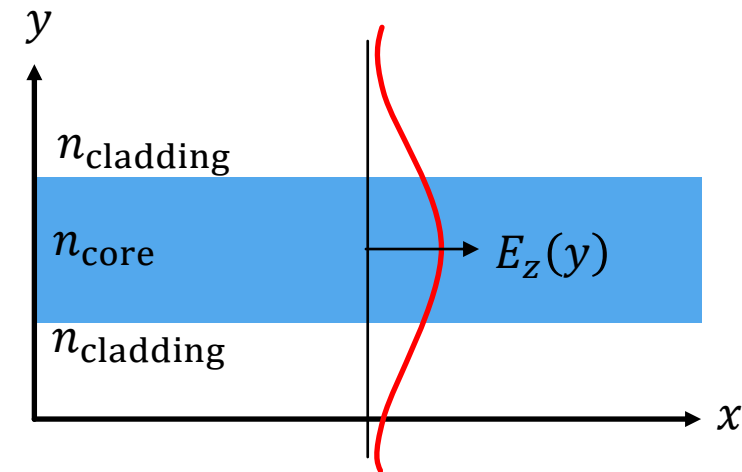


# Revision Wave Propagation

- Confinement

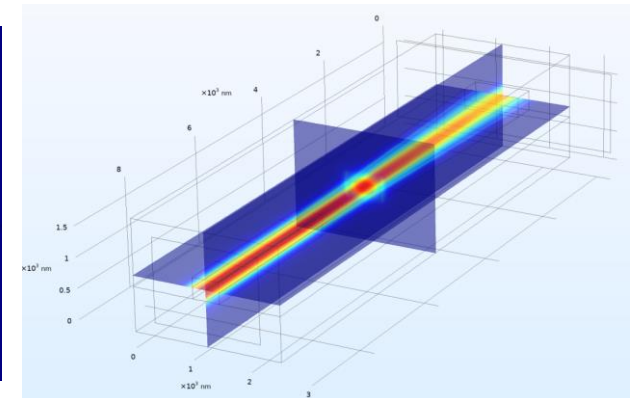
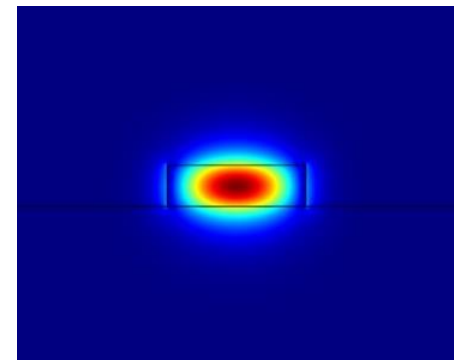
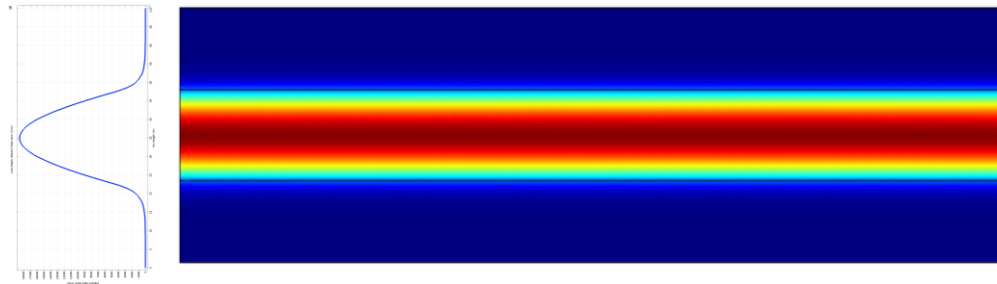
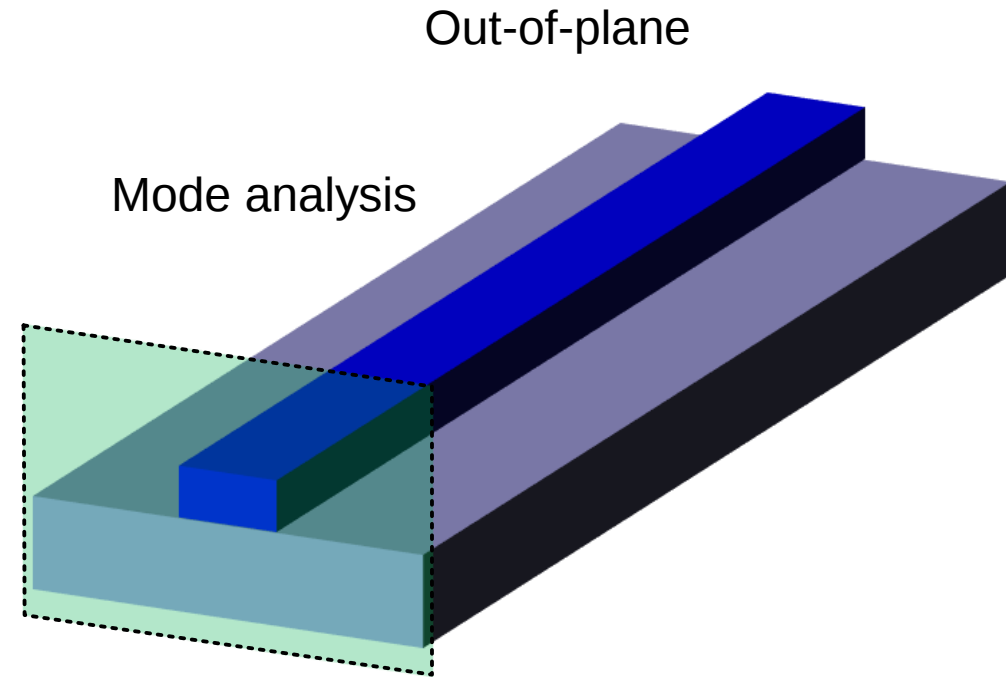
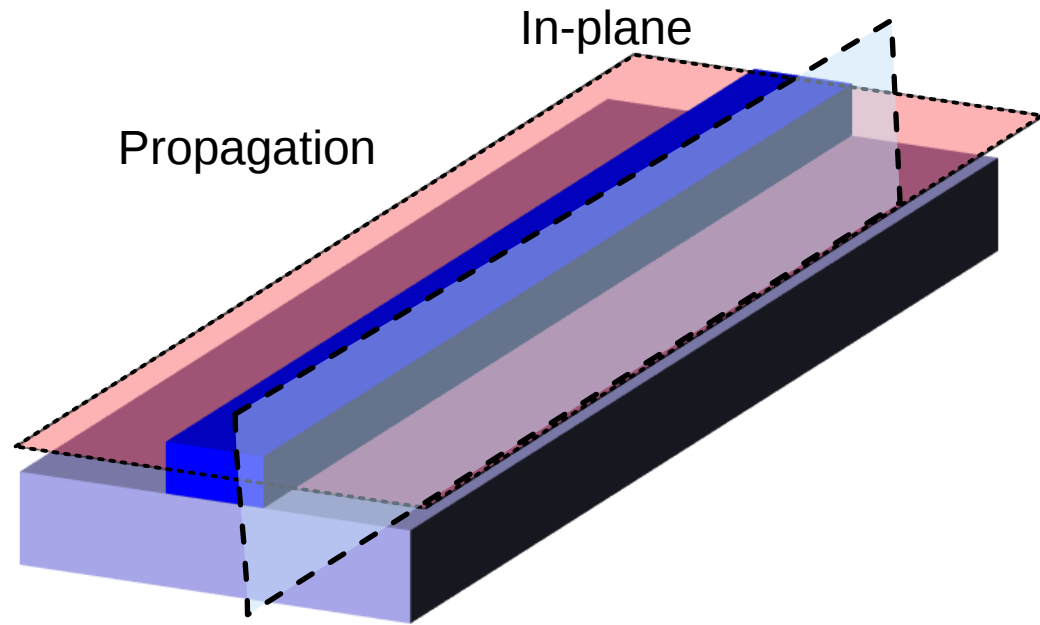


***Strongly confined***  
Wave mostly in the core



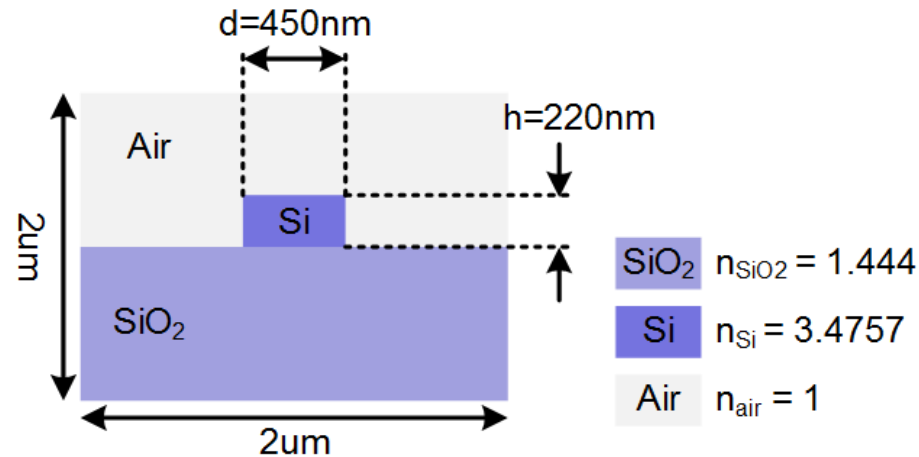
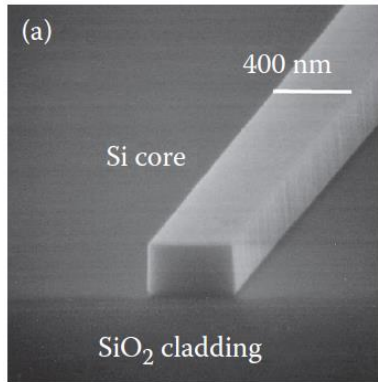
***Weakly confined***  
Wave leaks into cladding

# Revision Wave Propagation



# Revision Wave Propagation: Ridge Waveguide

- Multimode silicon ridge waveguide



## Given:

- $\lambda = 1550\text{ nm}$
- $n_{\text{Si}} = 3.47$
- $\text{Si}_{\text{Height}} = 220\text{ nm}$
- $\text{Si}_{\text{Width}} = [350, 1000]\text{ nm}$

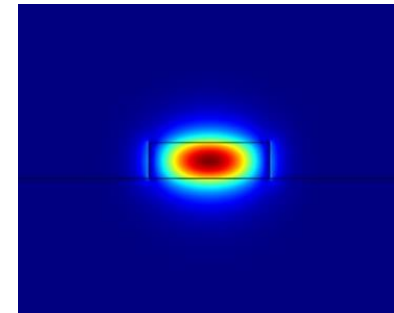
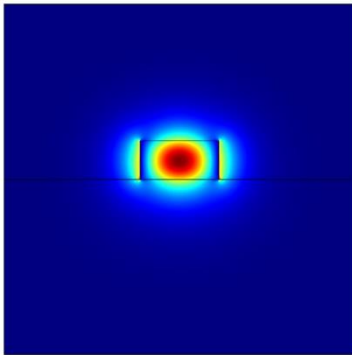
## Output:

- E-field (guided modes)
- Effective refractive index  $n_{\text{eff}}$

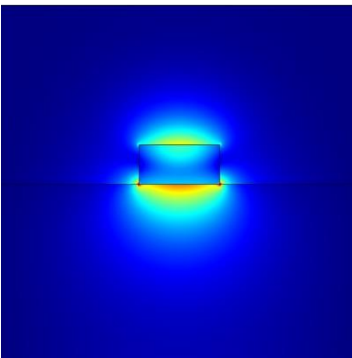
$$\begin{aligned}n_{\text{Si}} &= 3.4757 \\n_{\text{SiO}_2} &= 1.44 \\n_{\text{air}} &= 1\end{aligned}$$

# Revision Wave Propagation: Ridge Waveguide

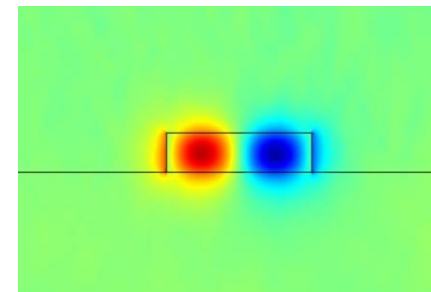
- Single-mode ridge
  - Solution 1:  $n_{\text{eff}} = 2.2719$
- Multi-mode ridge (increased geometry)
  - Fundamental mode



- Solution 2:  $n_{\text{eff}} = 1.5422$



- Higher order mode

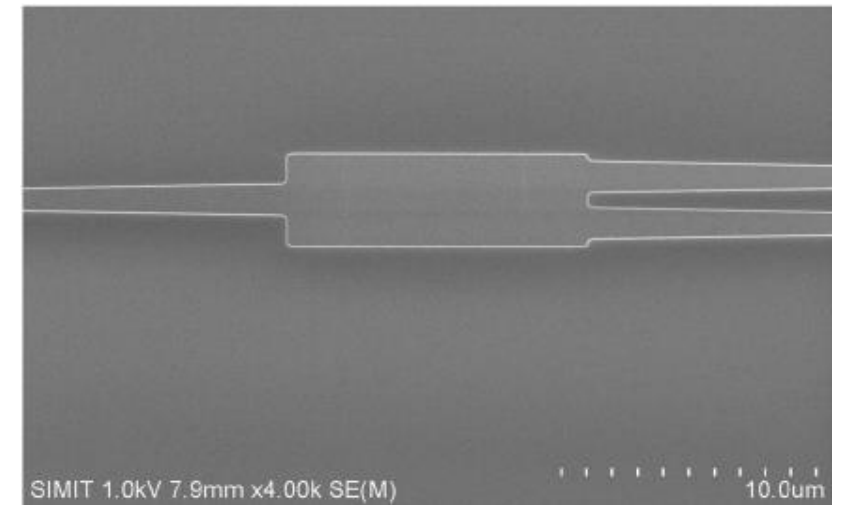
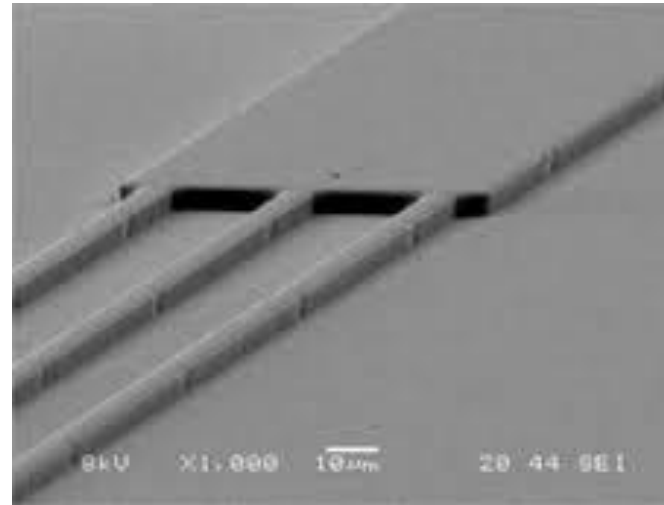


# Content

- Revision wave propagation
  - Waveguide
  - Confinement
  - Modes
- **S-parameters**
  - Theory
- **Projects**
  - Outline
  - Short overview projects
- **COMSOL examples**
  - Taper
  - Waveguide bend

# S-Parameters: Motivation

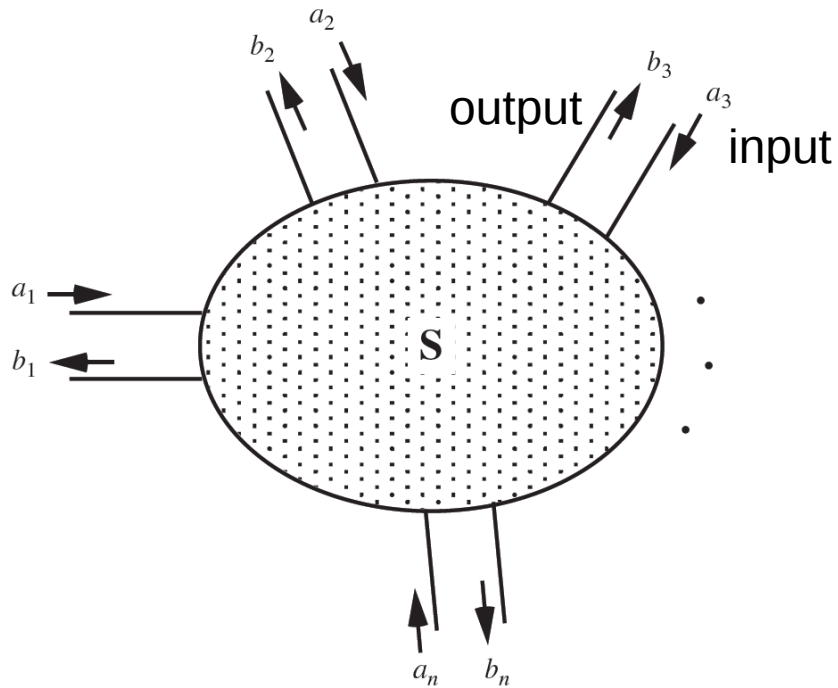
- What happens with systems for multiple inputs and multiple outputs (MIMO)?
- How can it be described mathematically?



- → We use the S-matrix

# S-Parameters for Photonics

- How to characterize our photonics system as whole?
  - Scattering matrix (so called S-matrix)



Superposition:

$$b_i = \sum_{j=1..n} S_{ij} a_j$$

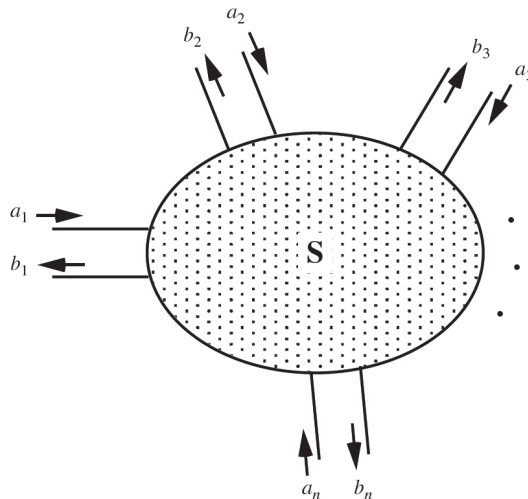
$$\begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_n \end{bmatrix} = \begin{bmatrix} S_{11} & \dots & S_{1n} \\ \vdots & \ddots & \vdots \\ S_{n1} & \dots & S_{nn} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_n \end{bmatrix}$$

# S-Parameters for Photonics

- How to characterize our photonics system as whole?
- S-matrix
  - Unitary in lossless systems
  - Diagonal  $S_{ii}$  terms are complex valued amplitude reflection coefficients

Superposition:

$$b_i = \sum_{j=1..n} S_{ij} a_j$$



$$\begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_n \end{bmatrix} = \begin{bmatrix} S_{11} & \dots & S_{1n} \\ \vdots & \ddots & \vdots \\ S_{n1} & \dots & S_{nn} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_n \end{bmatrix}$$

# S-Parameters for Photonics

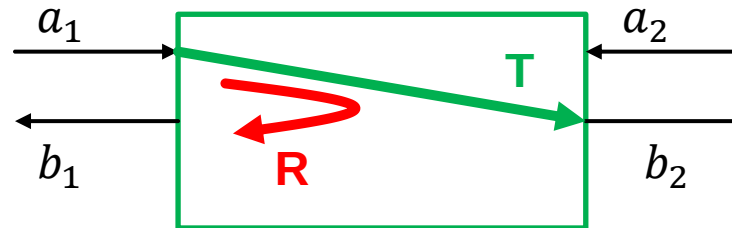
- How to characterize our photonics system as whole?
- S-matrix
  - Unitary in lossless systems
  - Diagonal  $S_{ii}$  terms are complex valued **amplitude reflection coefficients**

Two input/output ports:

$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$T =$

$R =$



# S-Parameters for Photonics

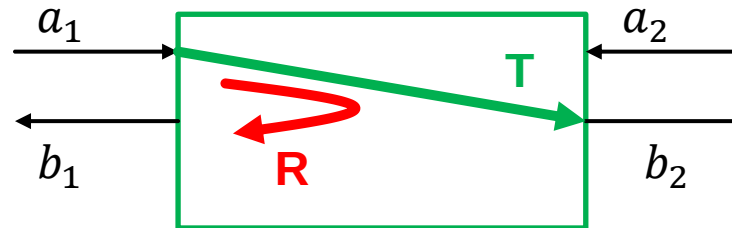
- How to characterize our photonics system as whole?
- S-matrix
  - Unitary in lossless systems
  - Diagonal  $S_{ii}$  terms are complex valued **amplitude reflection coefficients**

Two input/output ports:

$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$T = |S_{21}|^2$$

$$R = |S_{11}|^2$$



# S-Parameters for Photonics: COMSOL

- Can COMSOL help?
- S-matrix
  - Luckily, COMSOL has built-in calculation of these!

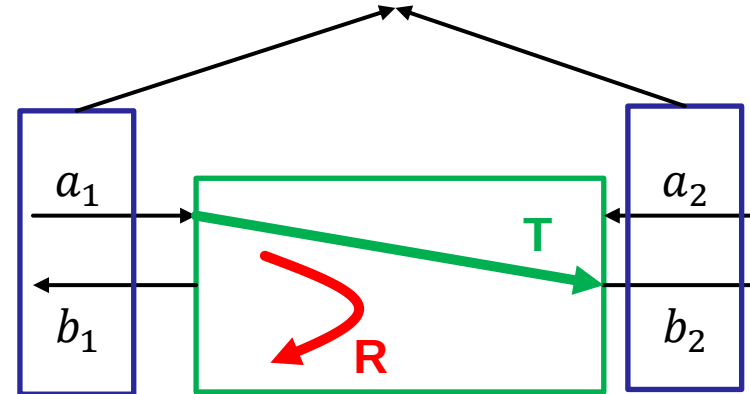
These are the ports we define in COMSOL!

Two input/output ports:

$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$T = |S_{21}|^2$$

$$R = |S_{11}|^2$$



COMSOL  
calculates this  
matrix!

# Content

- Revision wave propagation
  - Waveguide
  - Confinement
  - Modes
- S-parameters
  - Theory
- **Projects**
  - Outline
  - Short overview projects
- COMSOL examples
  - Taper
  - Waveguide bend

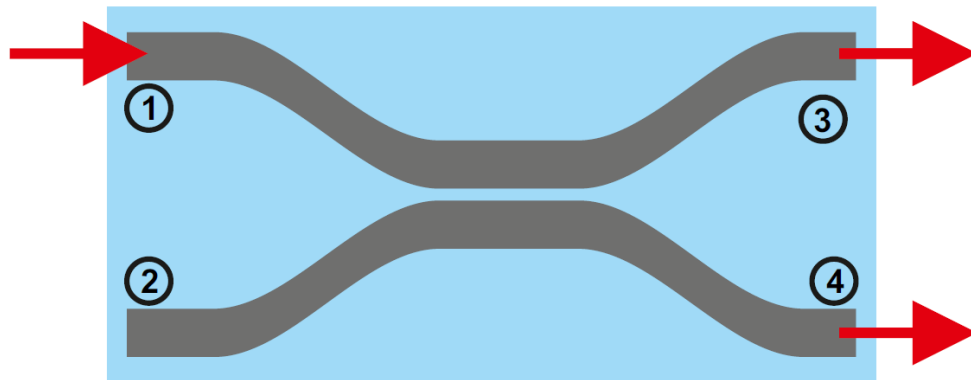
# Projects – Outline

| Date                 | Content                                                           |
|----------------------|-------------------------------------------------------------------|
| Mar 31 <sup>st</sup> | Description of all projects - Group Forming and start of projects |
| Apr 7 <sup>th</sup>  | Individual work on projects                                       |
| Apr 14 <sup>th</sup> | Individual work on projects                                       |
| Apr 21 <sup>st</sup> | EASTER BREAK - no lecture                                         |
| Apr 28 <sup>th</sup> | SECHSELÄUTEN – no lecture                                         |
| May 5 <sup>th</sup>  | Individual work on projects                                       |
| May 12 <sup>th</sup> | Individual work on projects / How to do presentations             |
| May 19 <sup>th</sup> | Working on projects & presentations                               |
| May 26 <sup>th</sup> | Presentations                                                     |

# Projects Overview

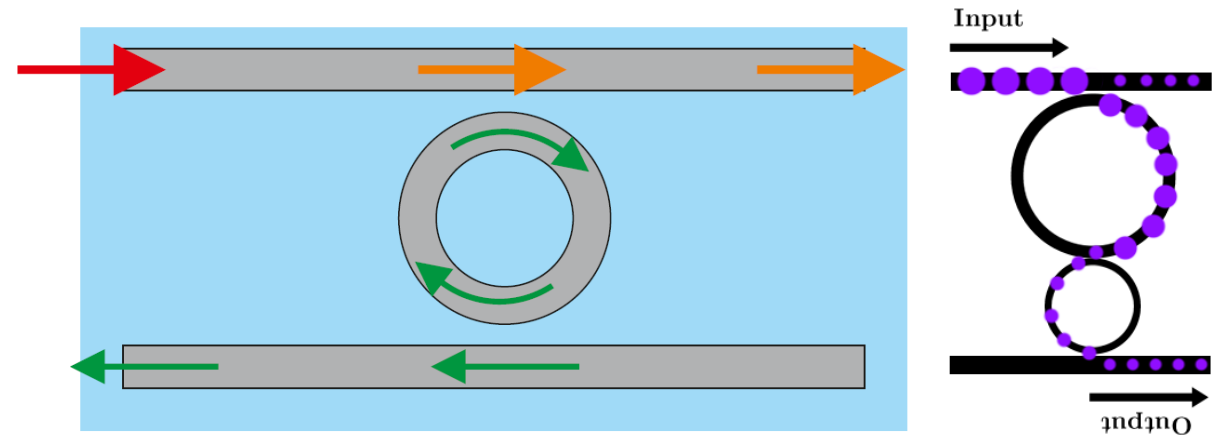
## ■ Directional coupler

- 2-3 students
- Goal
  - Analyze the Mode in 1D and 2D, discuss the difference
  - Wavelength: 1550 nm (C-Band)
  - Fix power ratio (to 50/50 and 90/10)
  - Minimize bending losses



## ■ Ring resonator

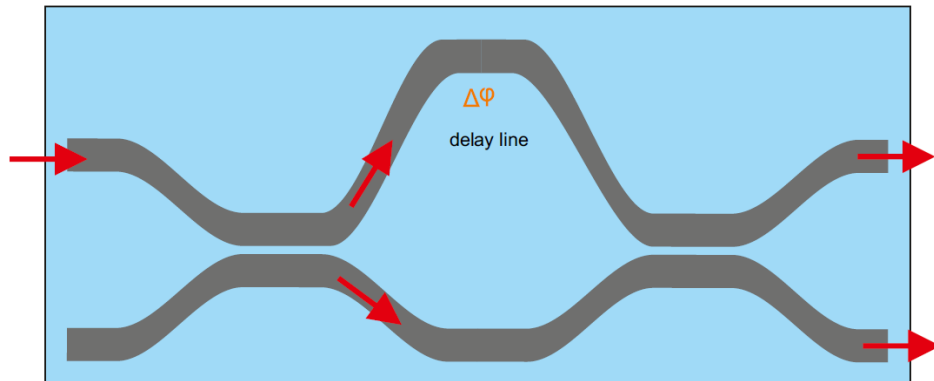
- 2-3 students
- Goal
  - Find the resonant behavior at 1550 nm
  - Maximize Q factor and minimize losses
  - Cascaded ring resonators for 60/40 ratio



# Projects Overview

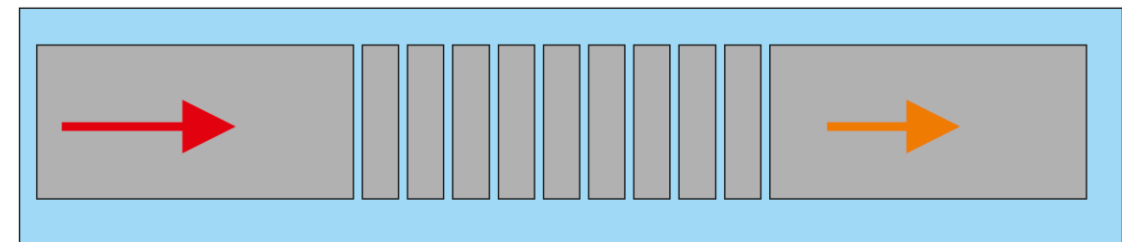
## ■ Delay interferometer

- 3 students
- Goal
  - Wavelength = 1550 nm
  - Minimize bending losses
  - Find delay line for  $\frac{\pi}{2}, \pi, 2\pi$  phase shift
  - Directional coupler or MMI for 50:50 ratio



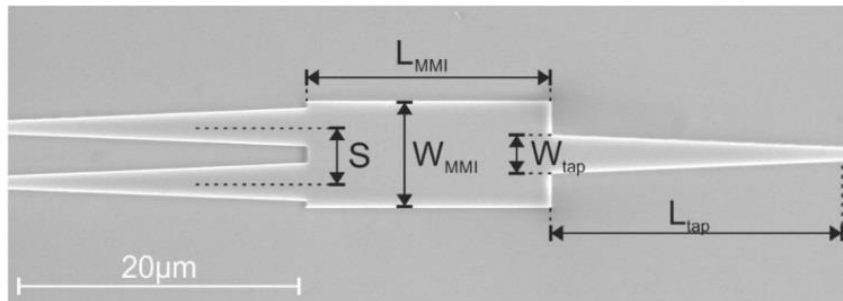
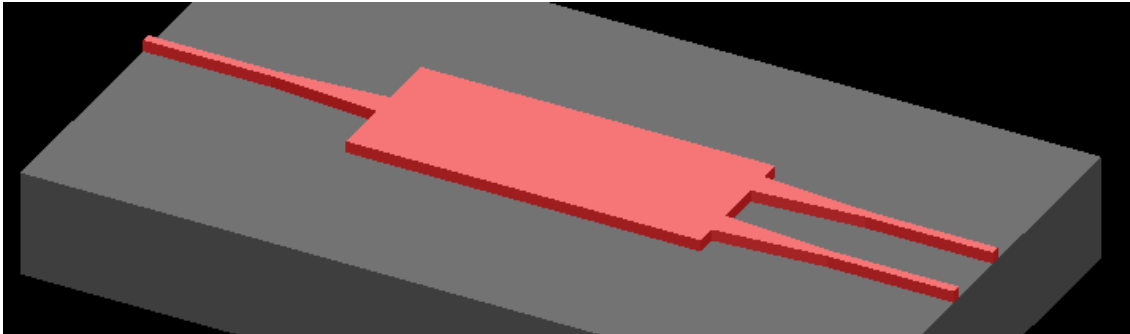
## ■ Bragg mirror

- 2-3 students
- Goal
  - Operating wavelength: 1550 nm
  - Incoming wave should be reflected,  $R > 0.9$  at 1550 nm
  - Reflection coefficient  $> 3$  dB for 1450-1650 nm

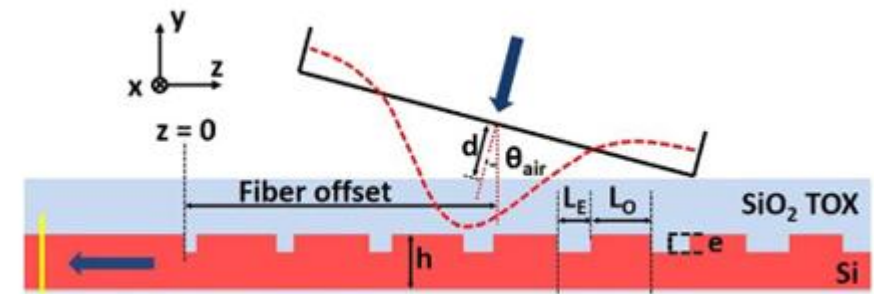


# Projects Overview

- **Multimode interferometer**
  - 2-3 students
  - Goal
    - Find geometry such that output ratio is 50/50 and also 10/90



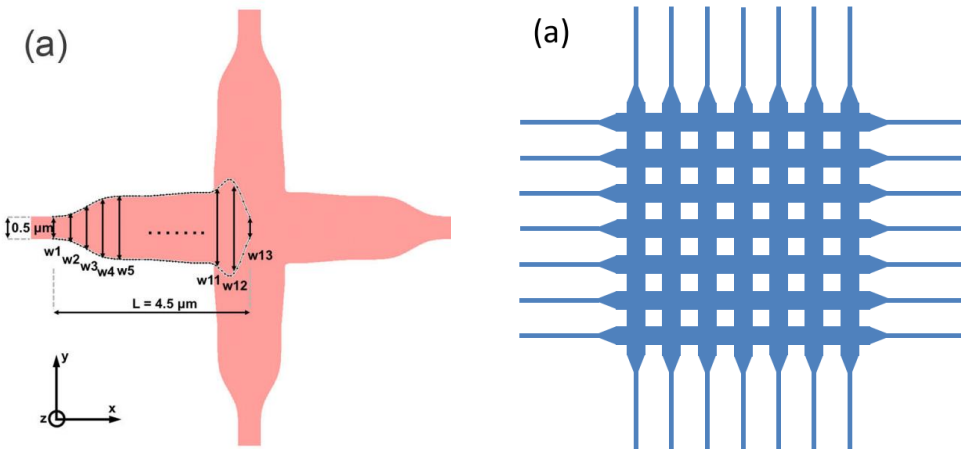
- **Grating Coupler**
  - 3 students
  - Goal
    - Simulate a grating coupler using the Bragg condition for a fiber incident angle of  $10^\circ$ .
    - Operating wavelength: 1550 nm
    - Maximize coupling efficiency from fiber to a certain mode inside the waveguide < 3 dB



# Projects Overview

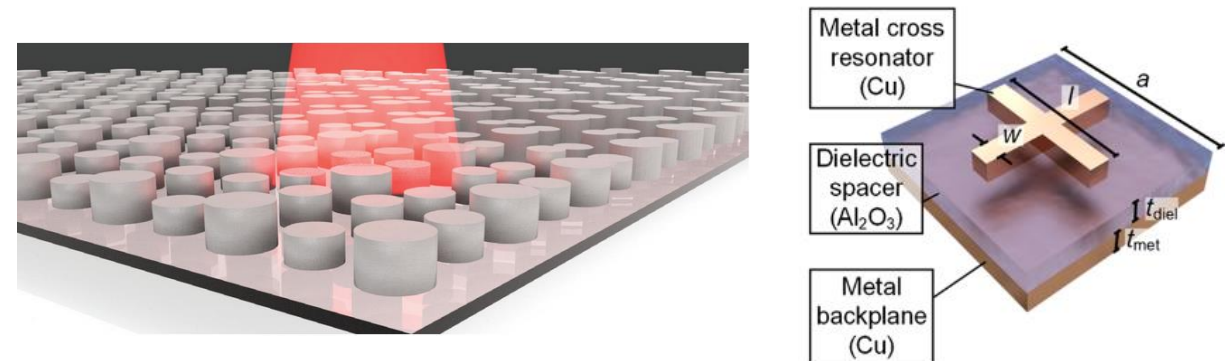
## ■ Waveguide Crossings

- 3 students
- Goal
  - Minimize transmission losses
  - Total losses < 0.3 dB



## ■ Metamaterial Perfect Absorber

- 3 students
- Goal
  - Design metamaterial perfect absorber based on the metal-insulator-metal layer stack
  - Analyze absorption spectra with respect to the peak position and FWHM
  - Analyze the polarization dependence
  - Operating wavelength: 2700 nm



# Projects Overview

- Your own ideas
  - They are WELCOME!
  - Please put together your ideas and make a small sketch by next week and let's have a look together

# Content

- **Revision wave propagation**

- Waveguide
- Confinement
- Modes

- **S-parameters**

- Theory

- **Projects**

- Outline
- Short overview projects

} Theory

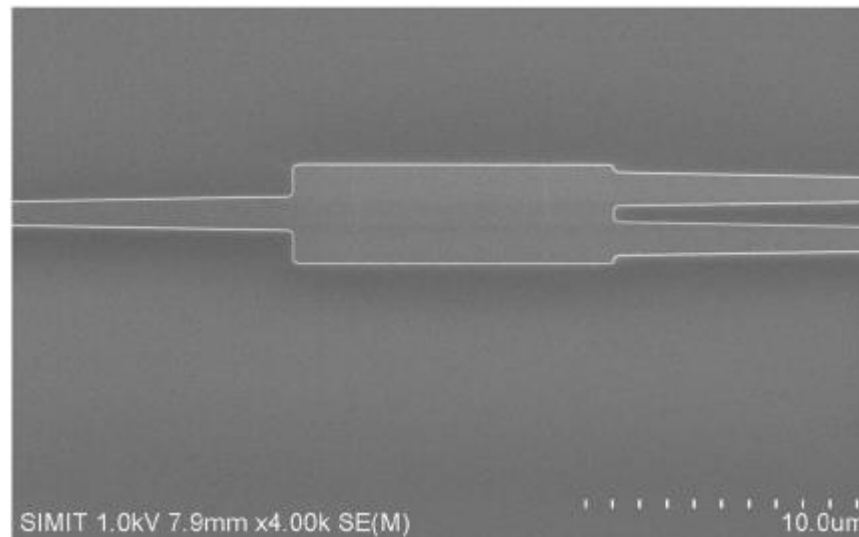
- **COMSOL examples**

- Taper
- Waveguide bend

} Tutorial

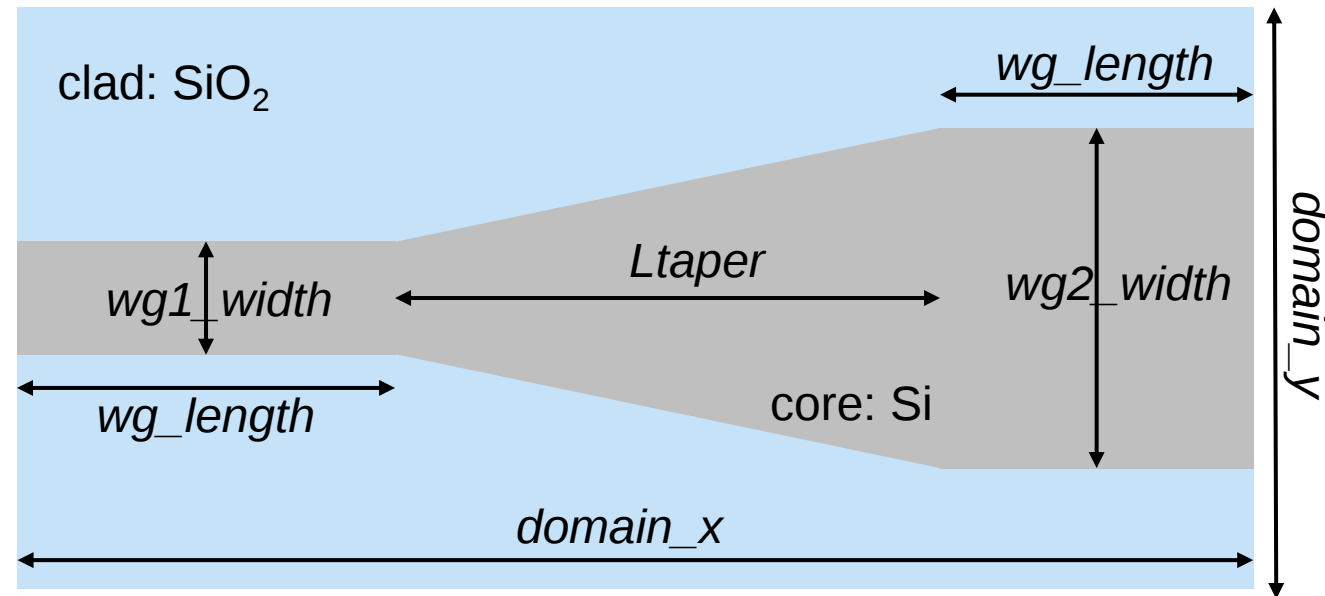
# COMSOL Examples: Taper

- “Tapering”
- Sometimes, photonics design requires that waveguide also changes its width...
- Example is Multi – Mode – Interference coupler (one of the projects)



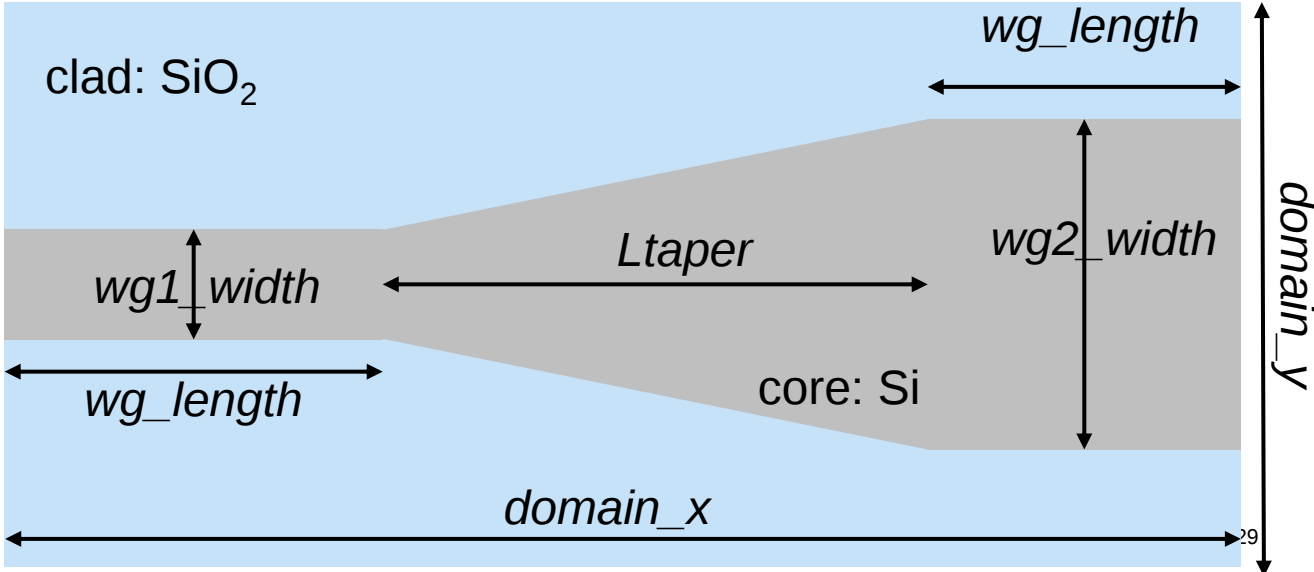
# COMSOL Examples: Taper

- Tasks:
  - Plot transmission curve for different taper lengths
    - (Note: you can **add trapezoid** or **polygon** in COMSOL)
    - $L_{\text{taper}}$  greater then 100 nm...



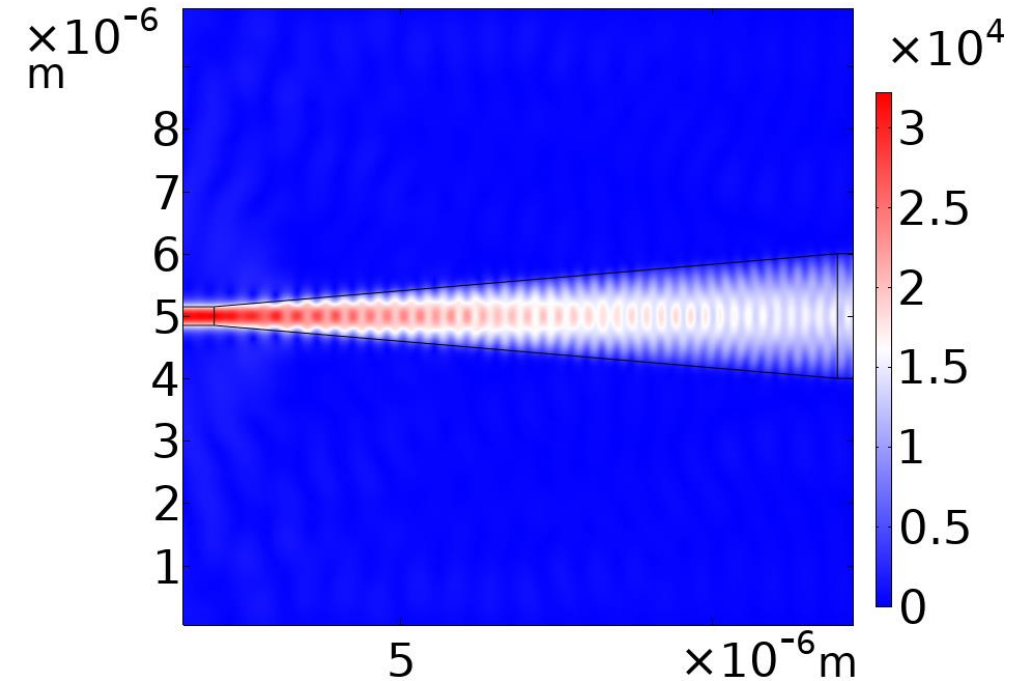


| Name      | Expression         | Value         | Description                |
|-----------|--------------------|---------------|----------------------------|
| lam0      | 1550[nm]           | 1.55E-6 m     | wavelength                 |
| f0        | c_const/lam0       | 1.9341E14 1/s | frequency                  |
| n_core    | 3.47               | 3.47          | index of Silicon           |
| n_clad    | 1.44               | 1.44          | index of Silicon Dioxide   |
| Ltaper    | 2[um]              | 2E-6 m        | taper length               |
| wg1_width | 300[nm]            | 3E-7 m        | 1st wg width               |
| wg2_width | 2[um]              | 2E-6 m        | 2nd wg width               |
| wg_length | 2[um]              | 2E-6 m        | waveguide straight lengths |
| domain_x  | 2*wg_length+Ltaper | 6E-6 m        | domain size in x           |
| domain_y  | 5*wg2_width        | 1E-5 m        | domain size in y           |



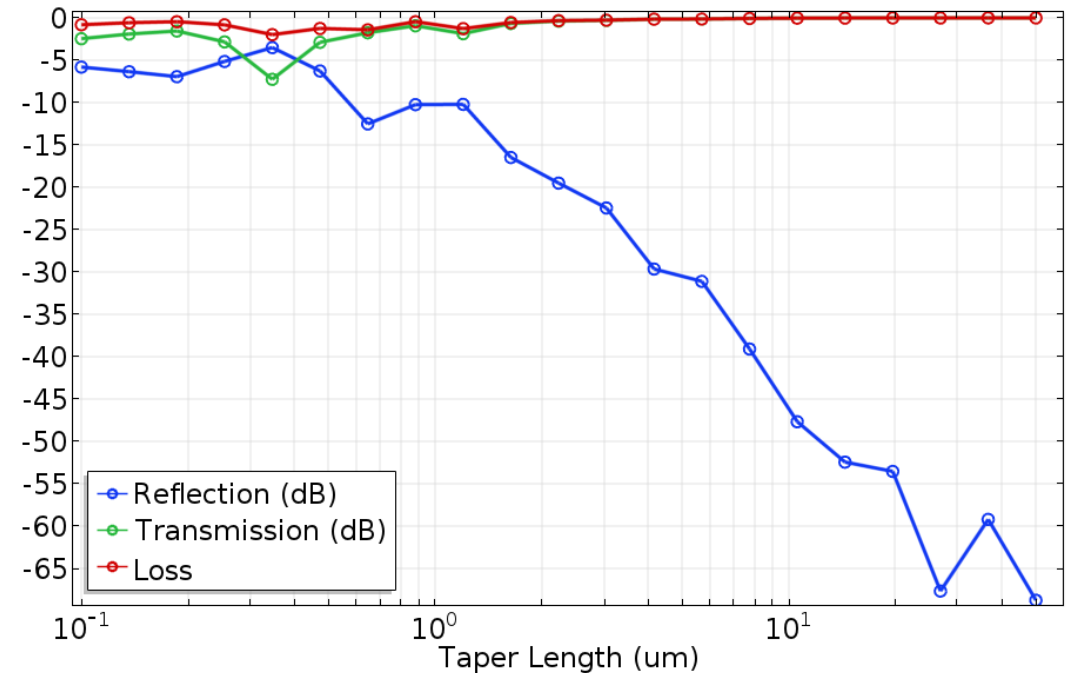
# Next Steps

- Define Materials
  - Cladding
  - Core
- Define Ports
  - Don't forget : Numeric
- Define Mesh
  - Not too small → computationally intensive
  - Too coarse → false results
- Select correct Study
  - Choose only one mode

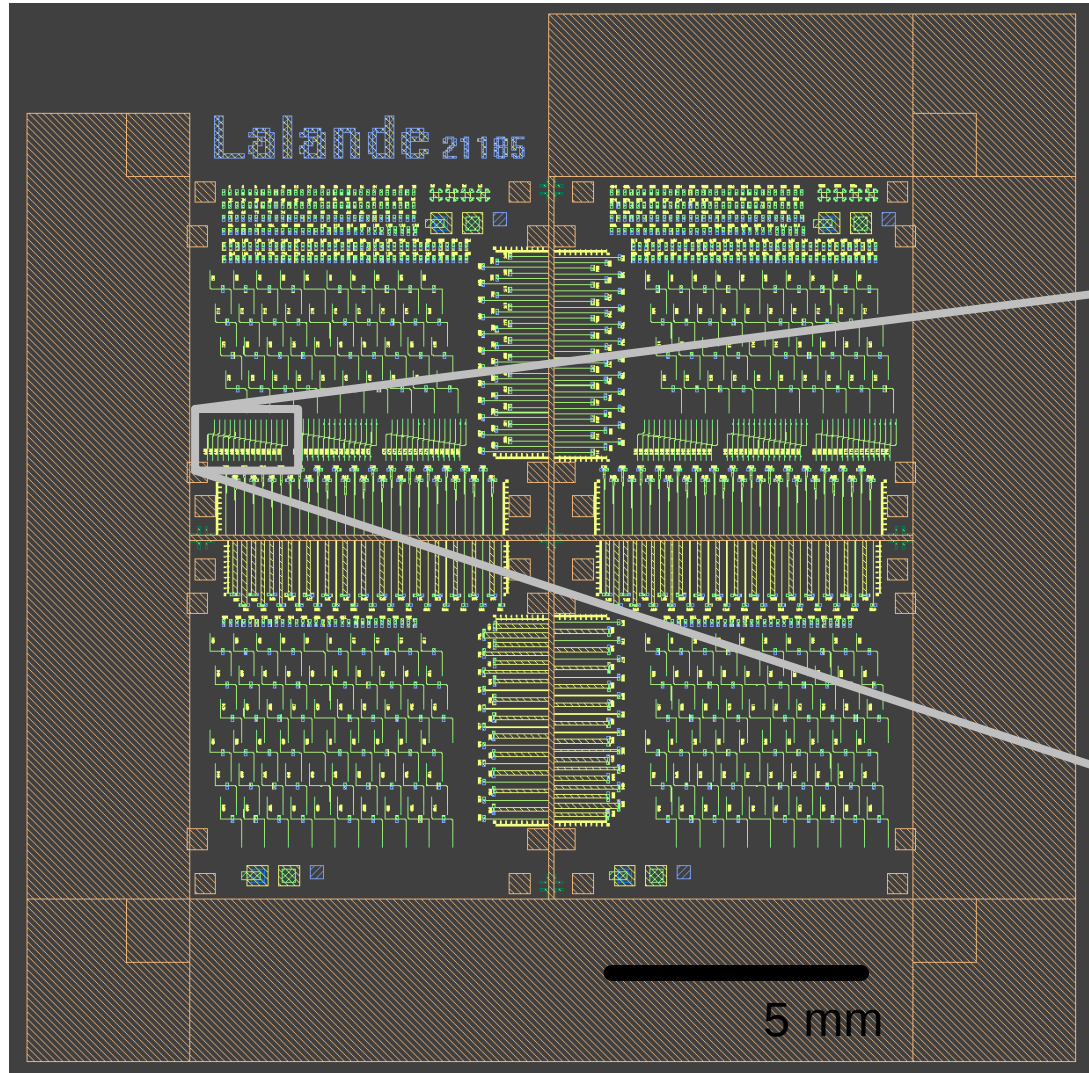


# Next Steps: Analyze S- Parameters

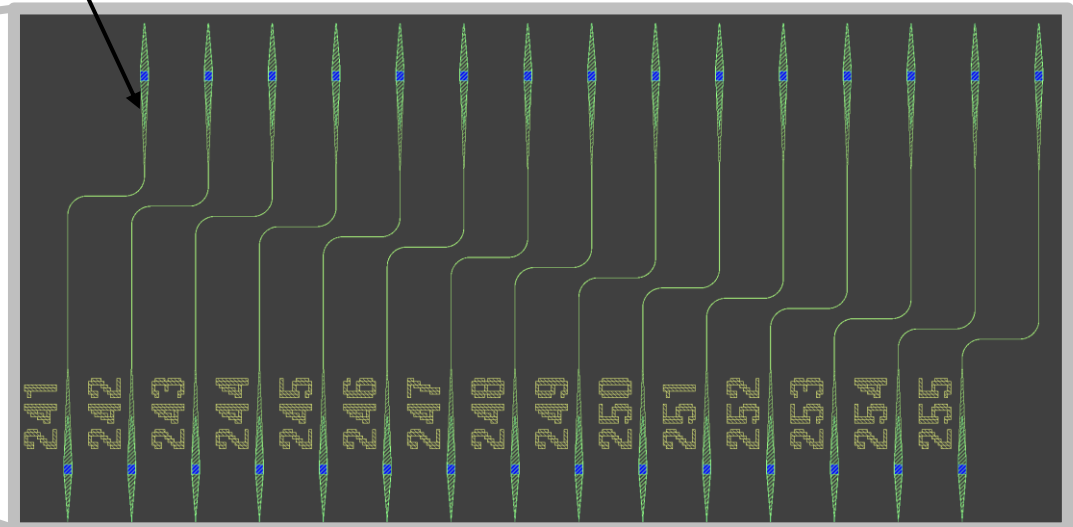
- Parameter sweep taper length
- S- Parameters can be used to plot
  - Reflection
  - Transmission
  - Losses
- Hint:
  - Derive desired S-parameter values  $S_{xx}$
  - Make a 1D- plot



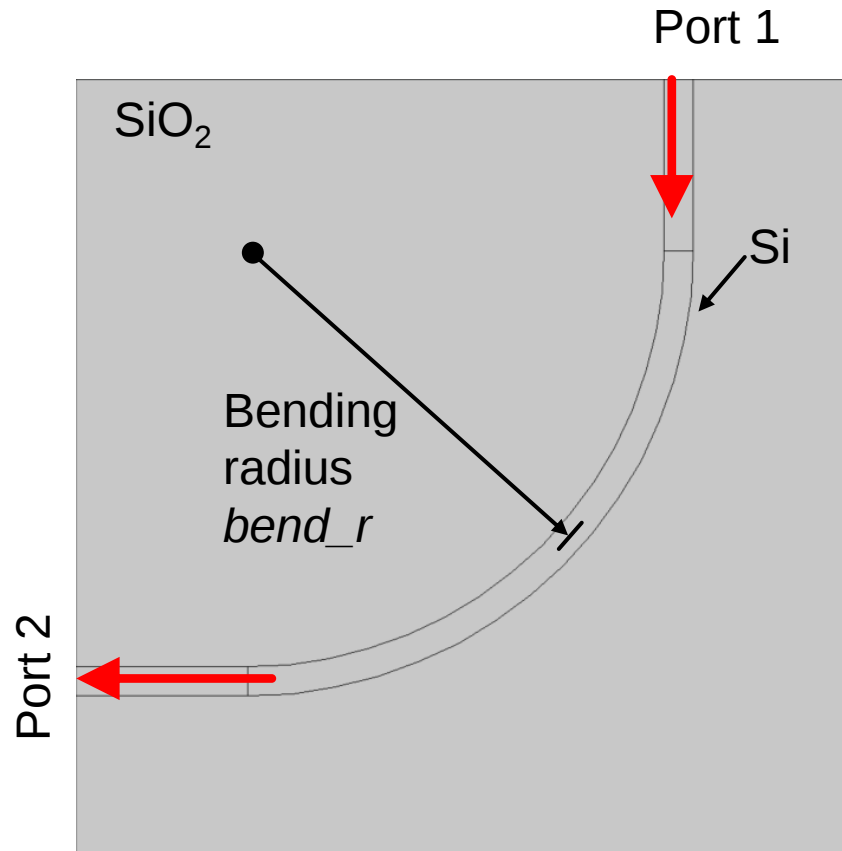
# Waveguide bending



Tapers

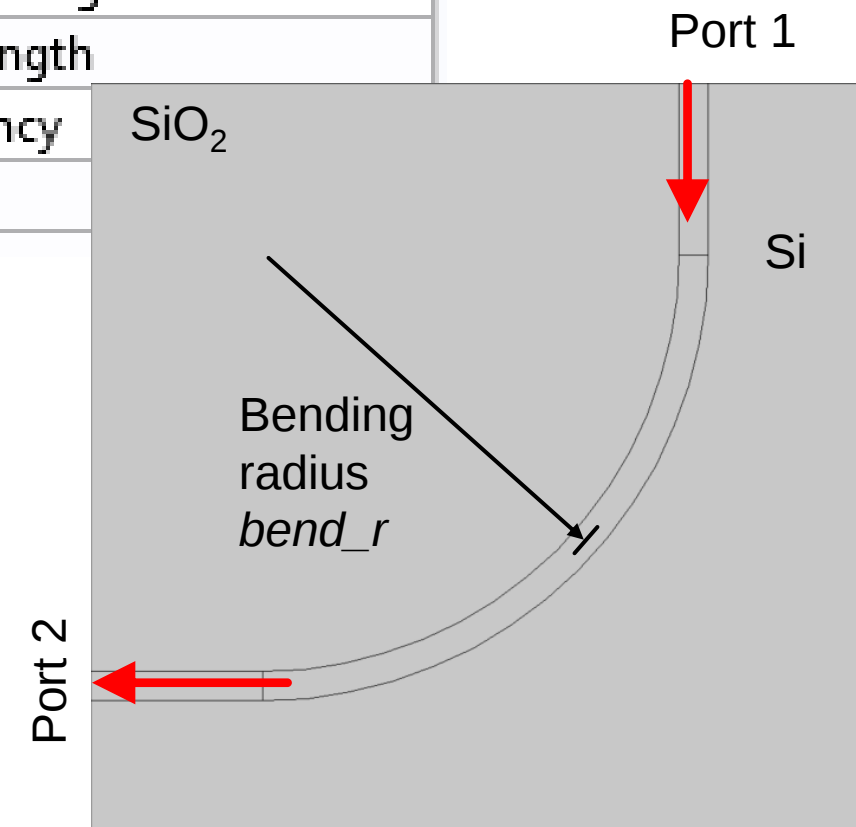


# S-Parameters for Photonics: COMSOL Waveguide Bend



- WG bend with a circular segment with a radius *bend\_r*
- *bend\_r* goes to the center of the WG
- We collect the power at port 2
- We calculate the transmission

| Name   | Expression     | Value         | Description     |
|--------|----------------|---------------|-----------------|
| bend_r | 0.5[um]        | 5E-7 m        | radius of bent  |
| Dx     | bend_r+2*si_in | 4.5E-6 m      | width domain    |
| Dy     | bend_r+2*si_in | 4.5E-6 m      | height domain   |
| si_in  | 2[um]          | 2E-6 m        | straight length |
| nSi    | 3.47           | 3.47          | Si index        |
| nSiO2  | 1.46           | 1.46          | SiO2 index      |
| wSi    | 450[nm]        | 4.5E-7 m      | width of wg     |
| lam0   | 1550 [nm]      | 1.55E-6 m     | wavelength      |
| f0     | c_const/lam0   | 1.9341E14 1/s | frequency       |
|        |                |               |                 |



# Next Steps

- Assign
  - Materials
  - Mesh
- Run simulation
- Evaluate transmission depending on
  - Radius
  - Wavelength

