



P&S COMSOL® Design Tool

Week 2: EM Introduction & Introduction to COMSOL

Manuel Kohli, Raphael Schwanninger

Content

- Recap

- Electromagnetics Introduction
 - Wavelength and Frequency
 - Spectrum
 - Maxwell's Equations
 - Wave Equation
 - Material Relations
 - Boundary Conditions

- COMSOL
 - Last Time
 - Today

Learning Objectives

- In this course, we aim to teach you the process of optical component design
- You will learn to:
 - ... **develop** a component idea into a specific design problem
 - ... **create** the correct simulation environment (model the photonic device)
 - ... **analyze** simulation results and **interpret** different physical effects involved
 - ... **evaluate** the design according to initial specifications and recommend improved solution
 - ... **summarize** the results and report them

Semester Outline

- Simulation concept
 - EM review
 - 2D EM simulation
- Intro to COMSOL tools
 - Wave optics
 - Mode solver
 - Boundary mode solver
- Project
 - Presentation
 - Report

6 weeks

6 weeks

Final presentation: Monday, 29.05.2023

Report : Monday, 05.06.2023

If there is a conflict, please let us know early

Practical Information – Administrative

- Time: Mondays from **13:15h** to **~15:00 h**
- Location: **ETZ D61.1**
- Our availability: office hours ETZ K-floor

(Send email to schedule a meeting)

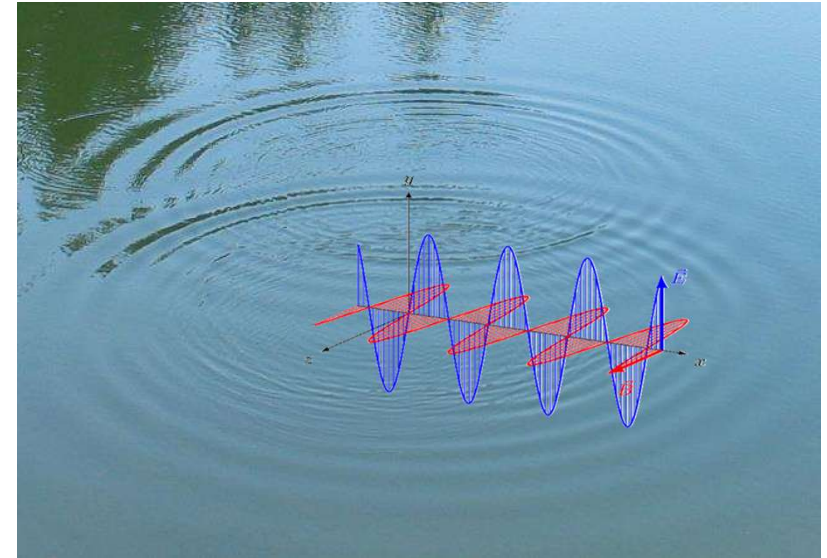
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Raphael	(ETZ K 60.1)	→ raphael.schwanninger@ief.ee.ethz.ch

About us

- Raphael Schwanninger
 - Mid- IR Photodetectors based on colloidal quantum dot materials
 - Metamaterials for absorption enhancement schemes
 - Simulation of different detector concepts
 - Fabrication of detectors with novel materials
- Manuel Kohli
 - Ferroelectric electro-optic modulators on SiN
 - Photonic integration of different platforms
 - Design, fabrication, and measurement
 - “Optical Machine” Assembly (PIC + EIC)
 - 3D Nanofabrication for novel components

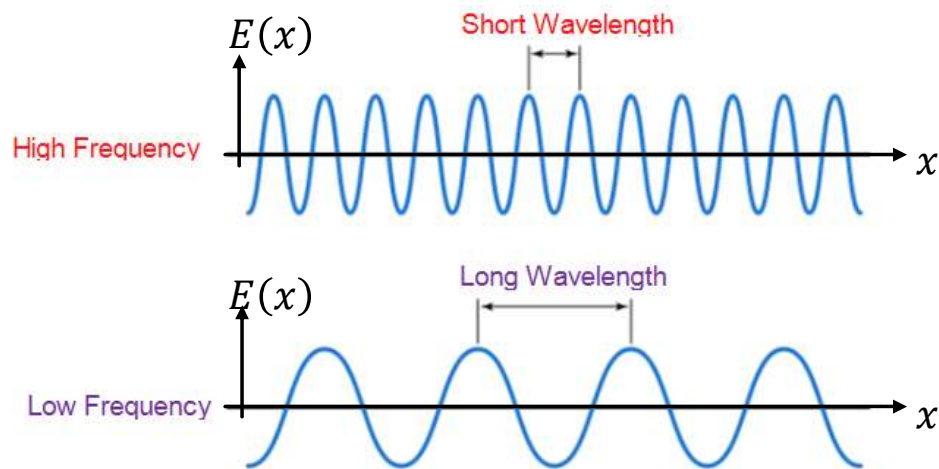
Motivation

- Wave behavior in nature
- But electromagnetic waves are (usually) invisible
- → COMSOL visualizes them!
- → Intuitive approach to understand mathematics
- Mathematics will be treated extensively in EM lectures

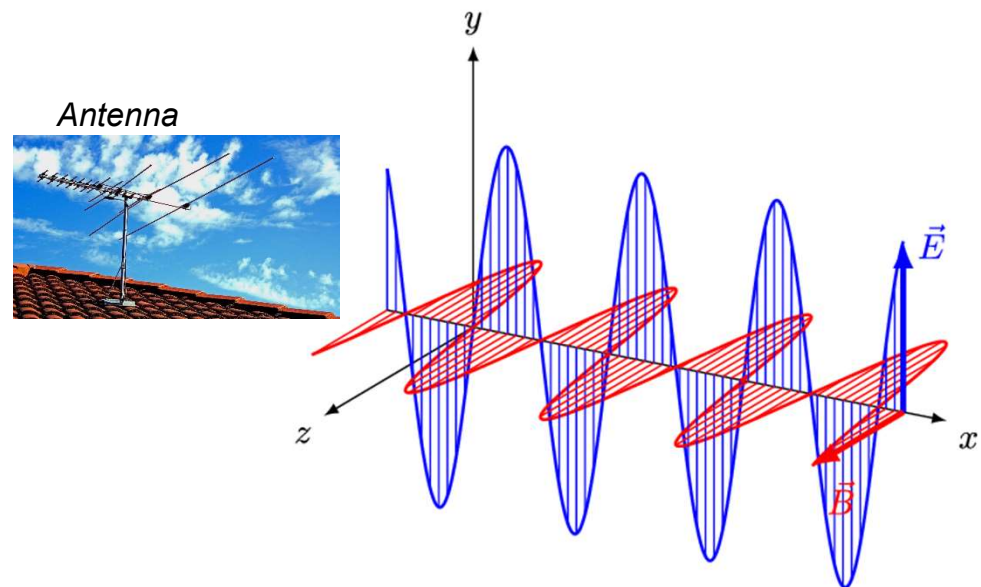


Electromagnetics: Wavelength and Frequency

- One moment in time, electric field:



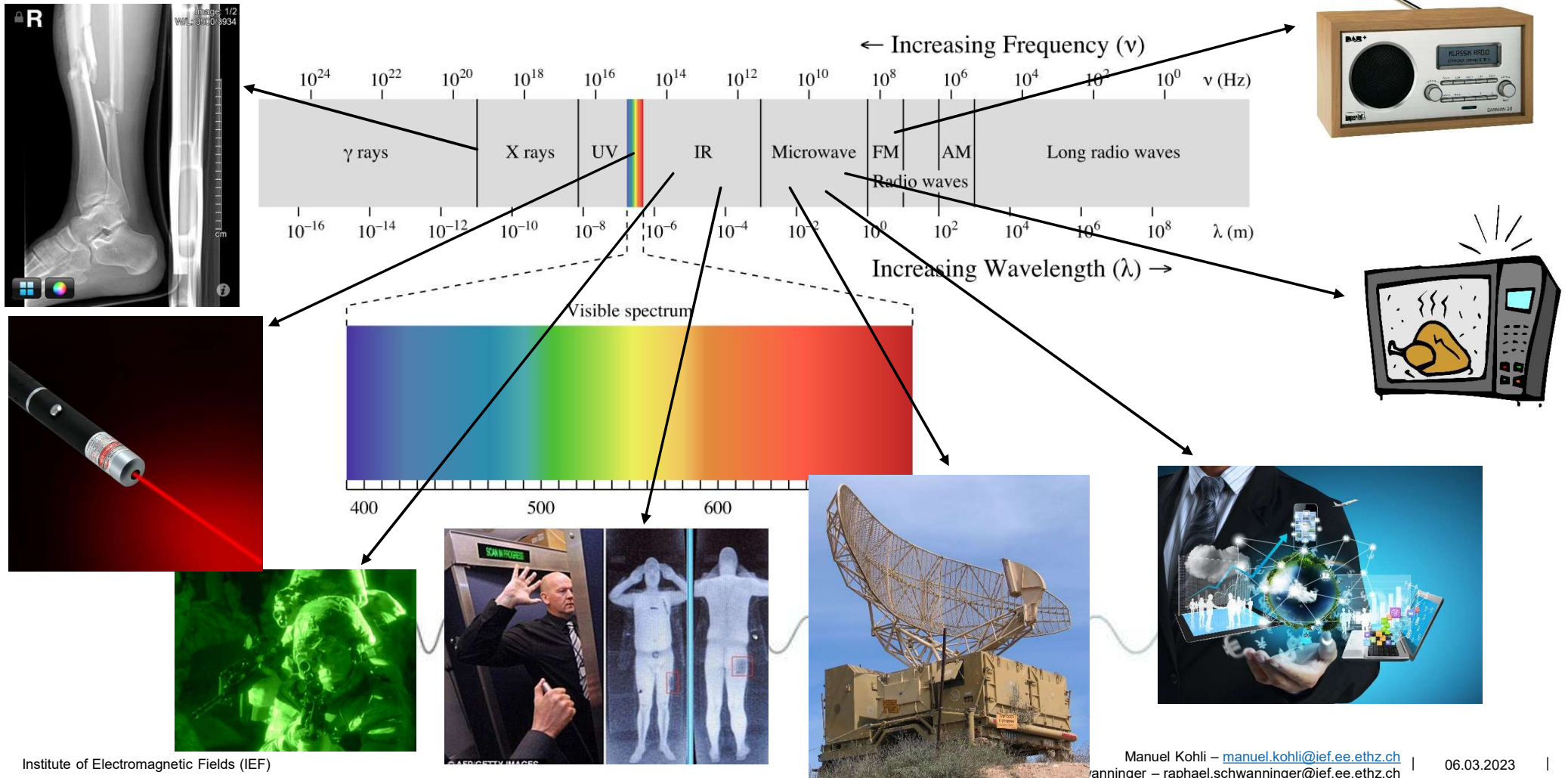
Let's see what happens over time:



- $f = \frac{c}{\lambda}$, c is the speed of light

→ Electric field vector changes in time and space

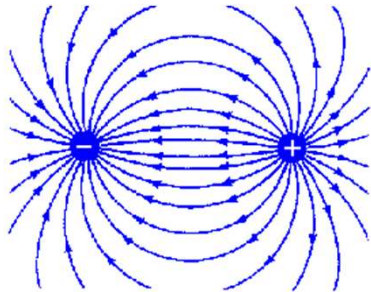
Electromagnetics in Our Daily Life



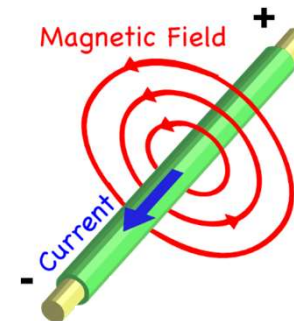
Electromagnetics: What you've seen before

- Physical phenomena and laws

Electric field between positive and negative charge

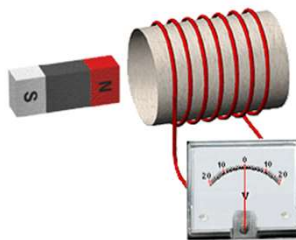


Current flows
→ magnetic field



Faraday's law of induction

$$u(t) = -\frac{d\Phi}{dt} = -\frac{d}{dt} \iint_A \vec{B} \cdot d\vec{A}$$



Coulomb force: $F = Eq$

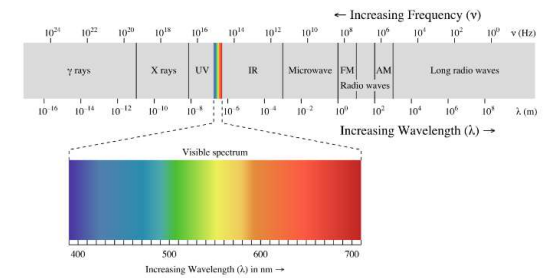
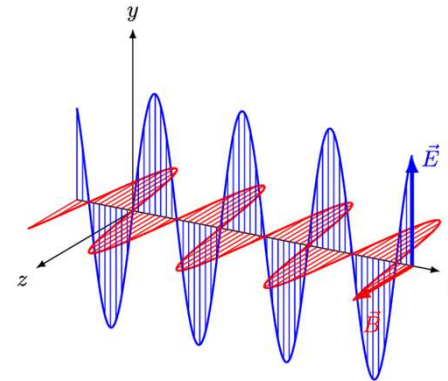
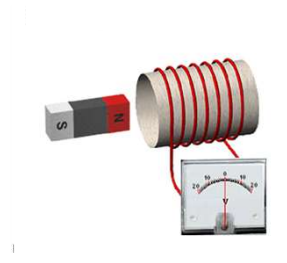
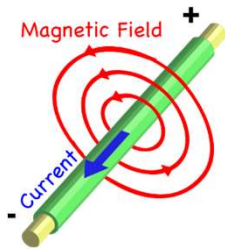
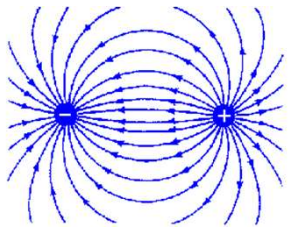
Ohmic law: $U = R \cdot I$

Kirchhoff current & voltage law:

$$\sum_{node} I_i = 0, \sum_{loop} U_i = 0$$

Electromagnetics: Maxwell's Equations

- All of these can be explained with

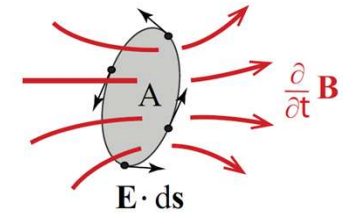


Only 4 equations ! $\rightarrow$ Maxwell's equations

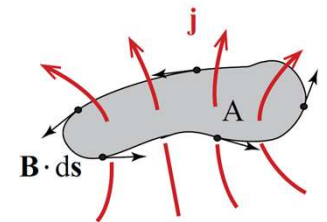
Electromagnetics: Maxwell's Equations

Electric field E

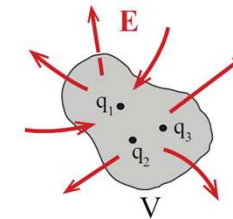
$$1. \quad \oint_{\partial A} E \, ds = -\frac{\partial}{\partial t} \int_A B \, dA$$

Magnetic field B Magnetic field H

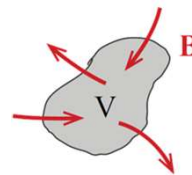
$$2. \quad \oint_{\partial A} H \, dl = \int_A \left(J + \frac{\partial D}{\partial t} \right) dA$$

Current density J Electric displacement Field D Electric displacement field D

$$3. \quad \oint_{\partial V} D \, dA = \int_V \rho \, dV$$

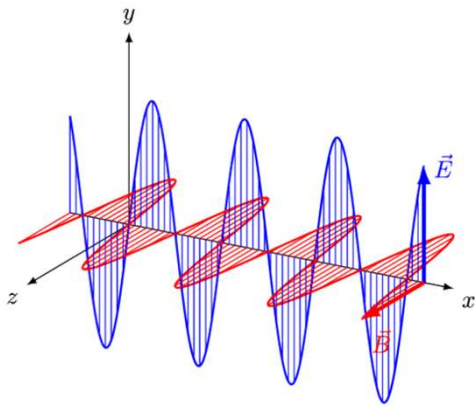
Charge density ρ Magnetic field B

$$4. \quad \oint_{\partial V} B \, dA = 0$$



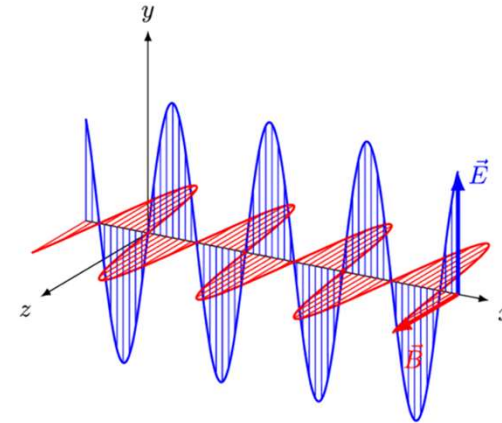
Electromagnetics: Maxwell's Equations

■ Electrodynamics



1. $\oint_{\partial A} \vec{E} \cdot d\vec{s} = -\frac{\partial}{\partial t} \int_A \vec{B} \cdot d\vec{A}$
2. $\oint_{\partial A} \vec{H} \cdot d\vec{s} = \int_A \left(\vec{J} + \frac{\partial \vec{D}}{\partial t} \right) \cdot d\vec{A}$
3. $\oint_{\partial V} \vec{D} \cdot d\vec{A} = \int_V \rho \, dV$
4. $\oint_{\partial V} \vec{B} \cdot d\vec{S} = 0$

■ Electrostatics (no change over time $\rightarrow \frac{\partial}{\partial t} = 0$)

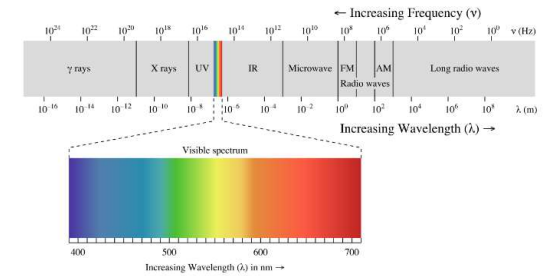
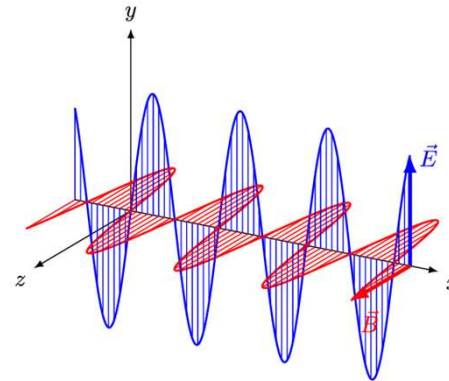
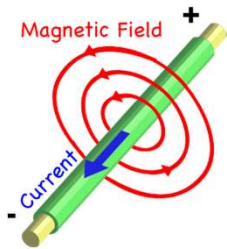
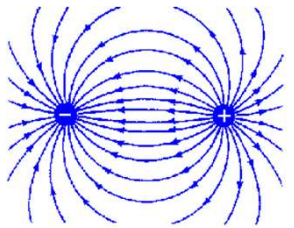


1. $\oint_{\partial A} \vec{E} \cdot d\vec{l} = 0$ (mesh rule)
2. $\oint_{\partial A} \vec{H} \cdot d\vec{l} = \int_A \vec{J} \cdot d\vec{A} = I$
3. $\oint_{\partial V} \vec{D} \cdot d\vec{A} = \int_V \rho \, dV$
4. $\oint_{\partial V} \vec{B} \cdot d\vec{S} = 0$



Electromagnetics: Maxwell's Equations

- All of these can be explained with



Only 4 equations ! → Maxwell's equations

- $\oint_{\partial A} \vec{E} \cdot d\vec{s} = -\frac{\partial}{\partial t} \int_A \vec{B} \cdot d\vec{A}$
- $\oint_{\partial A} \vec{H} \cdot d\vec{s} = \int_A \left(\vec{J} + \frac{\partial \vec{D}}{\partial t} \right) \cdot d\vec{A}$
- $\oint_{\partial V} \vec{D} \cdot d\vec{A} = \int_V \rho \, dV$
- $\oint_{\partial V} \vec{B} \cdot d\vec{A} = 0$

From Maxwell's equations the wave equation can be derived:

$$\frac{\partial^2 E_z}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 E_z}{\partial t^2} = 0$$

Electromagnetics: Materials Relations

- In order to analyze an EM problem we need to define the **material properties** involved
- Materials are defined by their **refractive index n** which is defined as

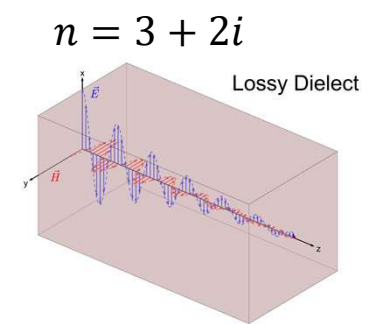
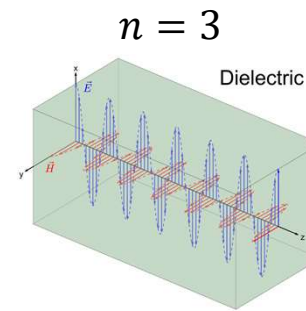
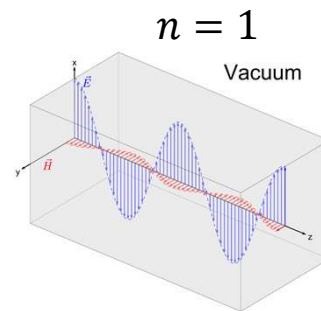
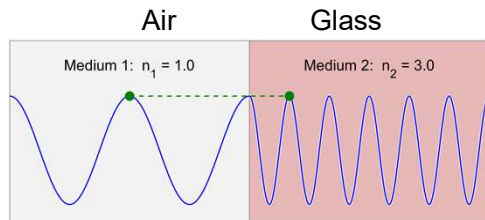
- $n = \sqrt{\mu_r \epsilon_r}$, for vacuum $n = 1$

- n is a complex number $n = n' + ik$

Influences wavelength

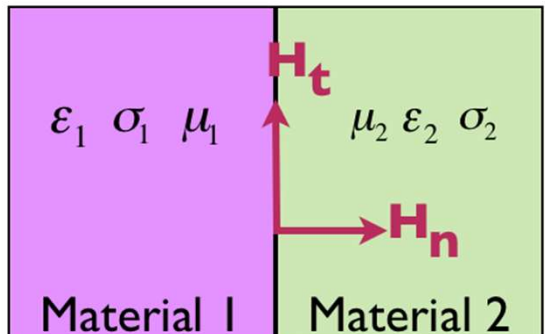
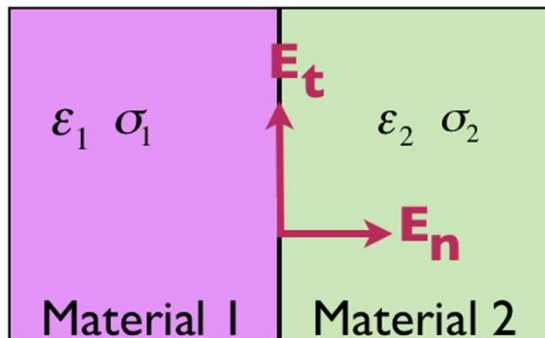
Influences losses

Antenna



Boundary Conditions

- Maxwell's Boundary Conditions



Boundary Conditions

$$E_{t,1} - E_{t,2} = 0$$

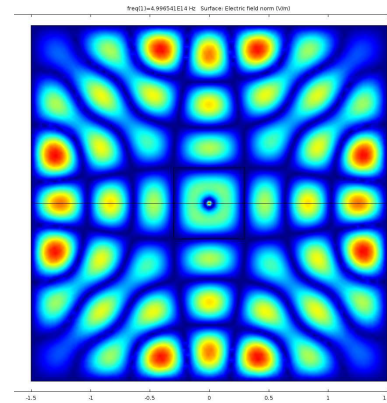
$$\epsilon_1 E_{n,1} - \epsilon_2 E_{n,2} = \sigma_f \text{ (surface charge density at the interface)}$$

$$H_{t,1} - H_{t,2} = J_s \text{ (surface current density at the interface)}$$

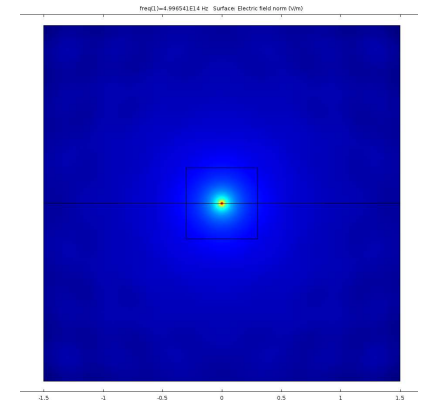
$$\mu_1 H_{n,1} - \mu_2 H_{n,2} = 0$$

COMSOL: Boundary Conditions

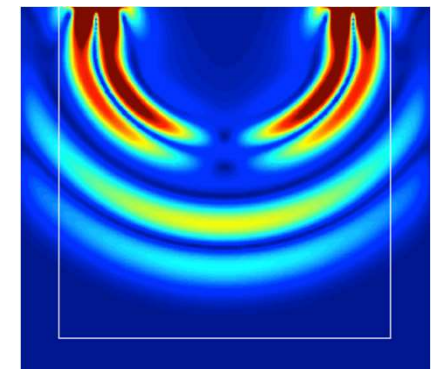
- Purpose of boundary conditions → define simulation domain
- Types of boundary conditions in COMSOL
 - Perfect Electric Conductor (PEC)
 - Perfect Magnetic Conductor (PMC)
 - Scattering Boundary Condition
 - Periodic Boundaries Condition (PBC)
 - Perfectly Matched Layer (PML)



PEC Boundaries



Scattering Boundaries



PML Boundaries

COMSOL: Boundary Conditions

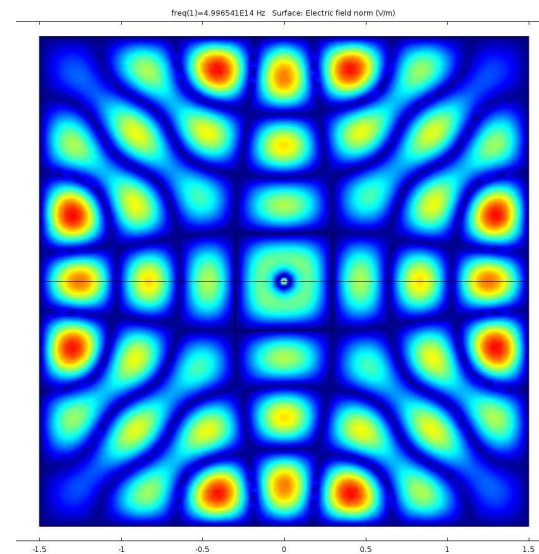
- **Perfect Electric Conductor (PEC)**

- Properties

- Electric field cannot penetrate → reflection of electric field
 - Equivalent to infinite electric conductivity

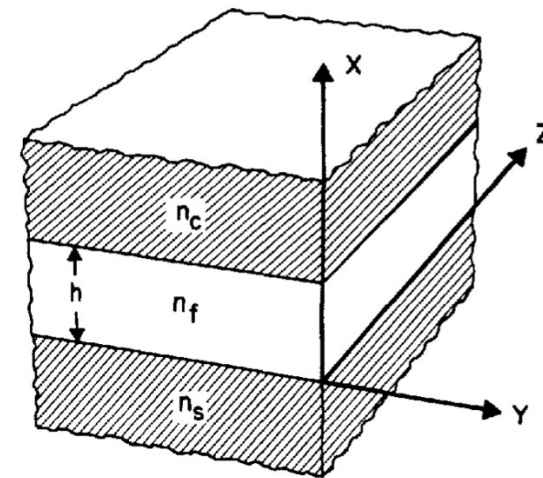
- Examples

- Microwave planar structures
 - Metallic substrates
 - Short circuit interface
 - To implement some certain symmetry



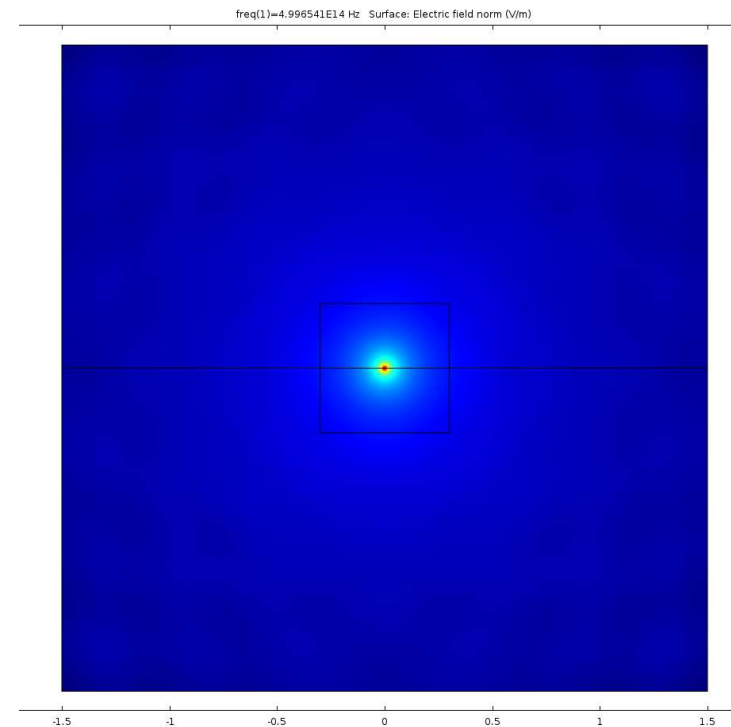
COMSOL: Boundary Conditions

- **Perfect Magnetic Conductor (PMC)**
 - Properties
 - Magnetic field cannot penetrate → reflection of magnetic field
 - Equivalent to infinite magnetic conductivity
 - Examples
 - To account for certain symmetry
 - Interface between dielectric and air
 - Open circuit interface



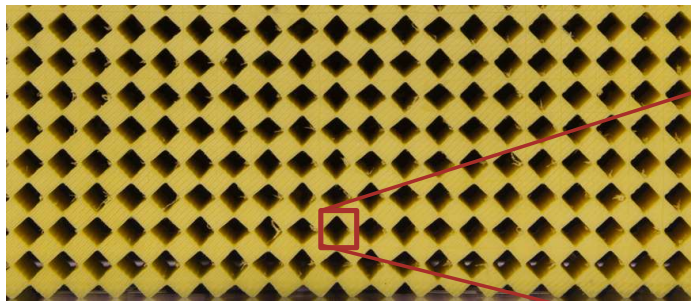
COMSOL: Boundary Conditions

- **Scattering Boundary Condition**
 - Properties
 - Electric field is absorbed $\rightarrow$ no reflection
 - Examples
 - To simulate an “infinite” domain
 - As we did last time with the point source

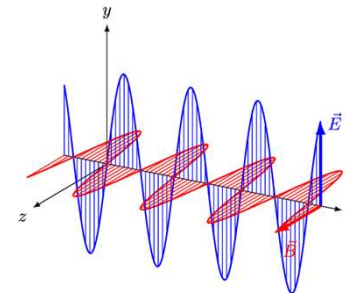
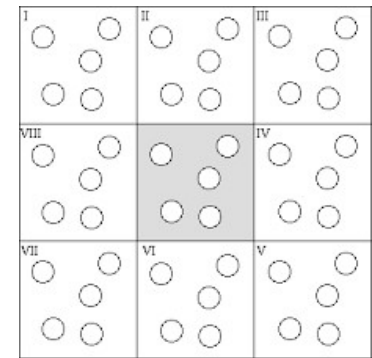


COMSOL: Boundary Conditions

- **Periodic Boundary Condition**
 - For repeating structures
 - Use a unit cell for the analysis
 - Simulates systems expanding infinitely in 1D/2D



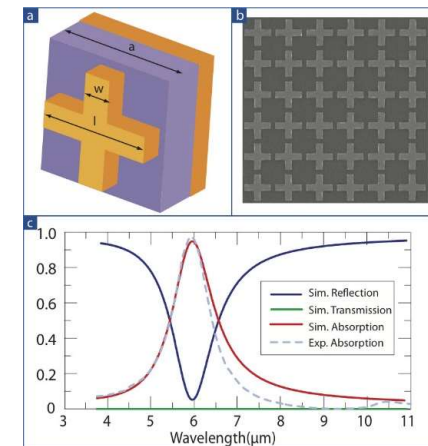
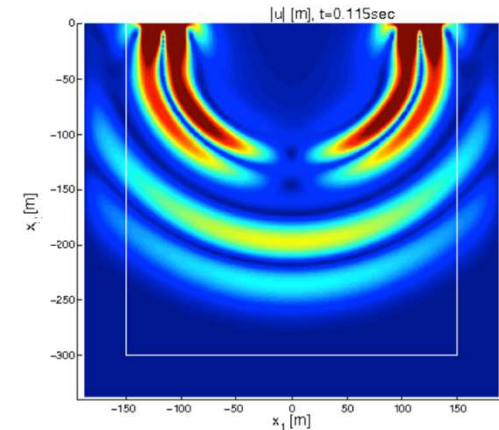
Periodic Boundaries



COMSOL: Boundary Conditions

- **Perfectly Matched Layer (PML)**
 - Scattering Boundary
 - Properties
 - Absorbing boundary
 - Truncates EM space in numerical simulations.
 - Possible to simulate open boundary problems.
 - Reduce scattered/reflected waves.

- **Examples**
 - Antennas
 - Reflectors
 - Absorbing structures
 - Metamaterials



Real life absorber

Starting COMSOL

- Every Student has access to Linux Server

Connection to Linux Server

1) Download and install Cisco Anyconnect: <https://ethz.ch/content/dam/ethz/special-interest/hest/isg-hest-dam/documents/pdf/vpn-de.pdf>

Available for MS,MAC & Linux

2) Connect to ETH network using Ciso Anyconnect

3) Connect to Linux Server

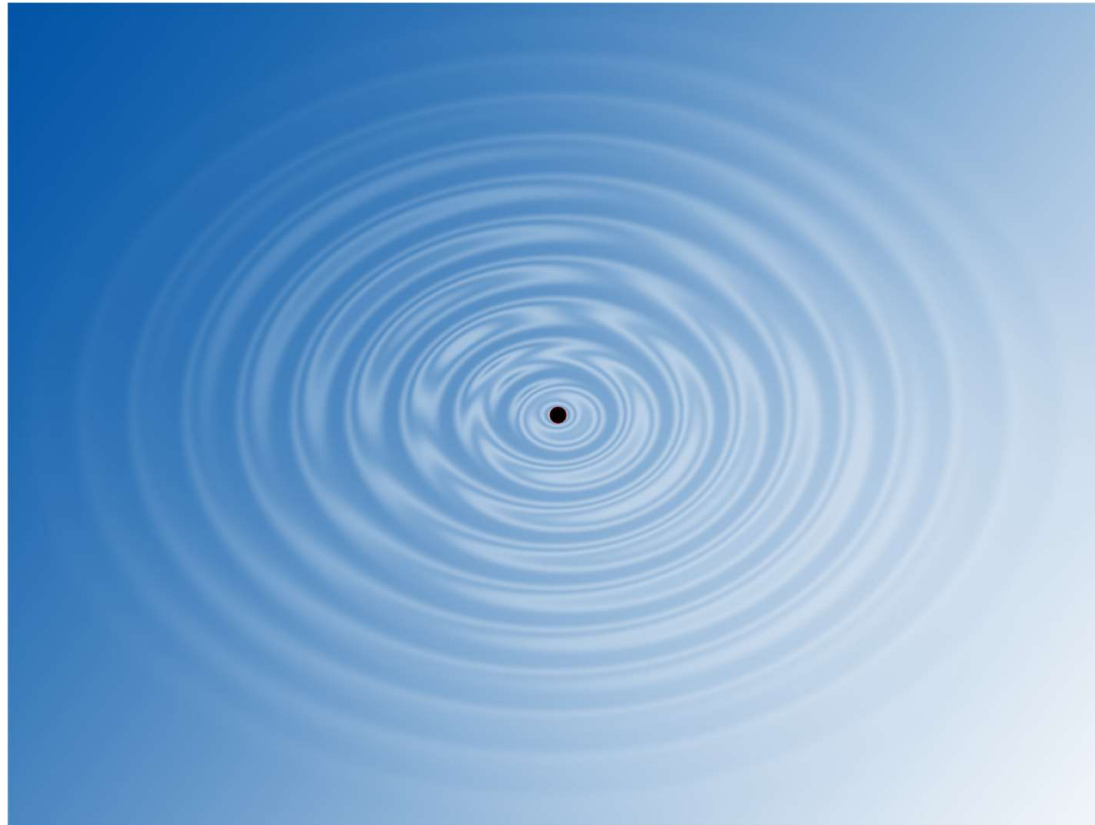
- Linux & Mac: using terminal type «ssh [\\$username@itet-ief-l0.ethz.ch](mailto:$username@itet-ief-l0.ethz.ch) -X»
- Windows, Linux, Max: using any remote desktop with xserver capability (e.g. Remmina)

4) Enter Username and Password

5) Start COMSOL

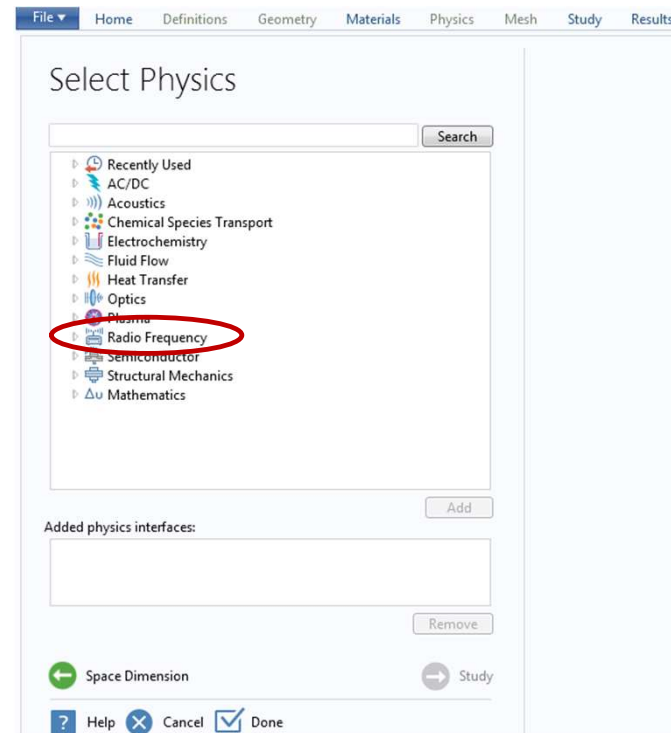
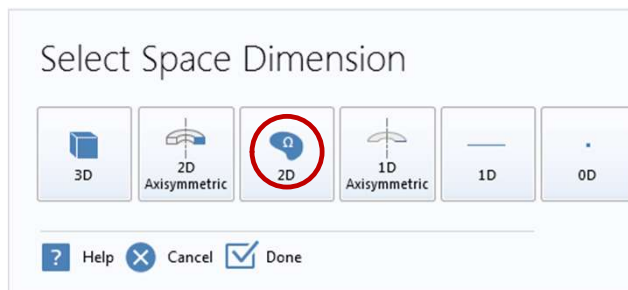
type: «comsol &» into the terminal

COMSOL: Last Time – Point Source Field

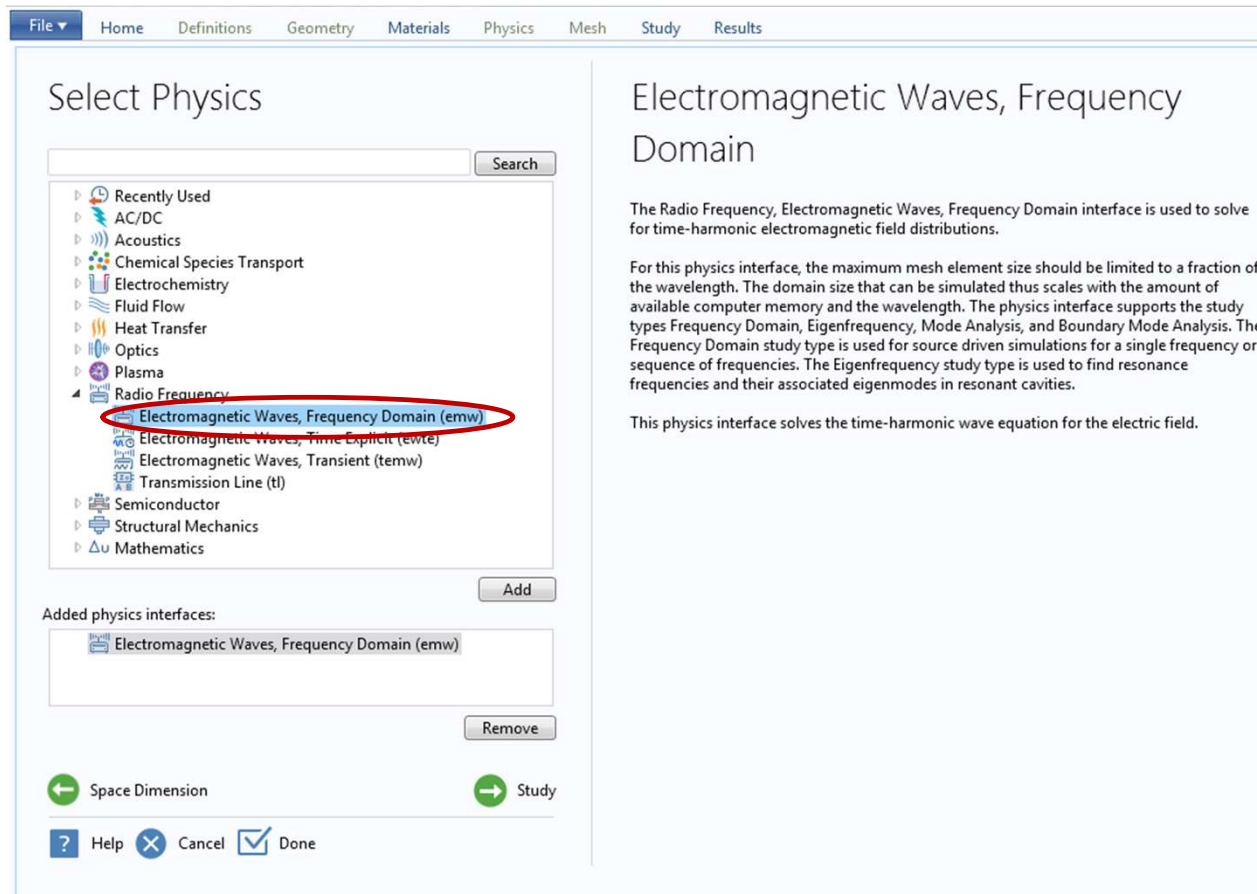


COMSOL: Last Time

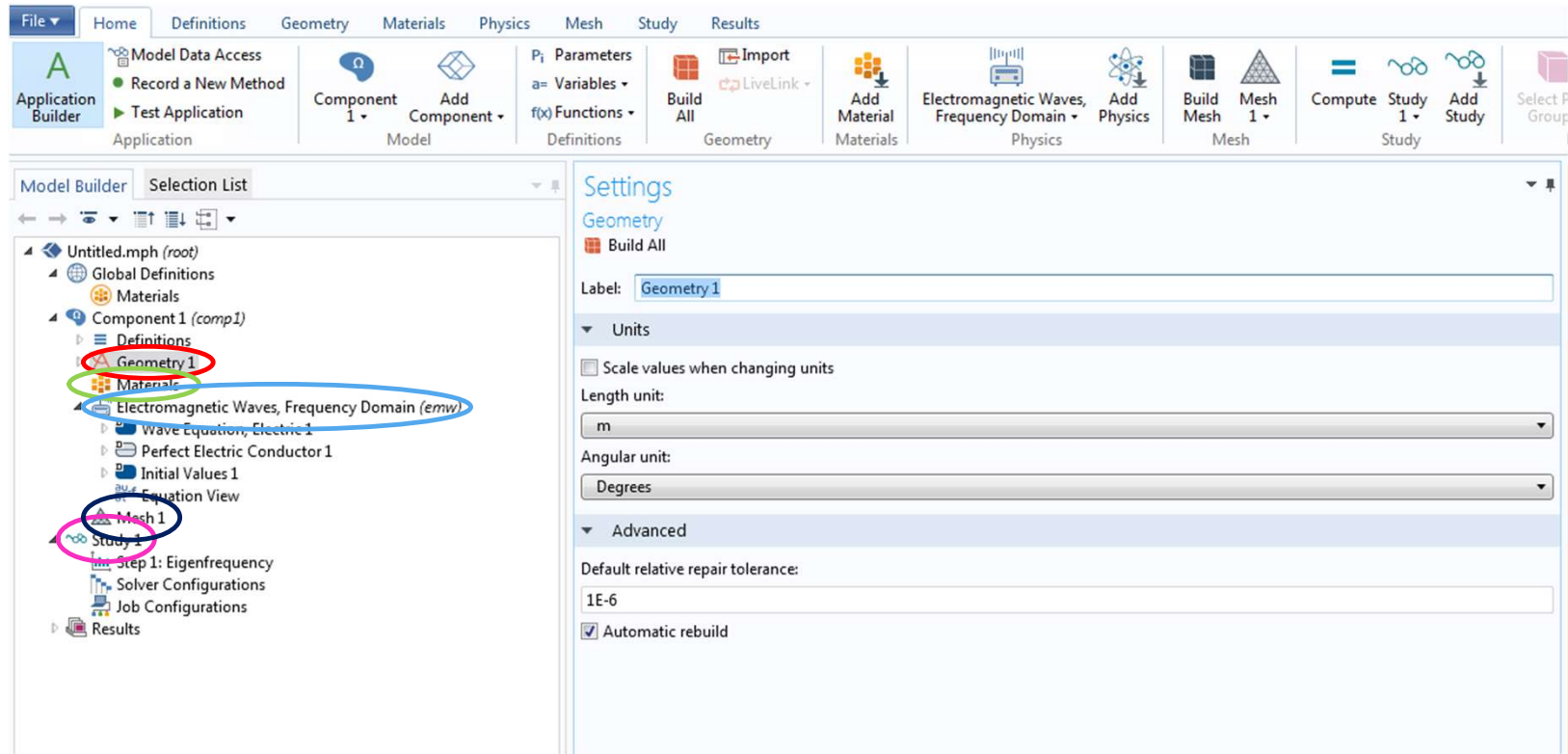
Command to start Comsol: **comsol**



COMSOL: Last Time

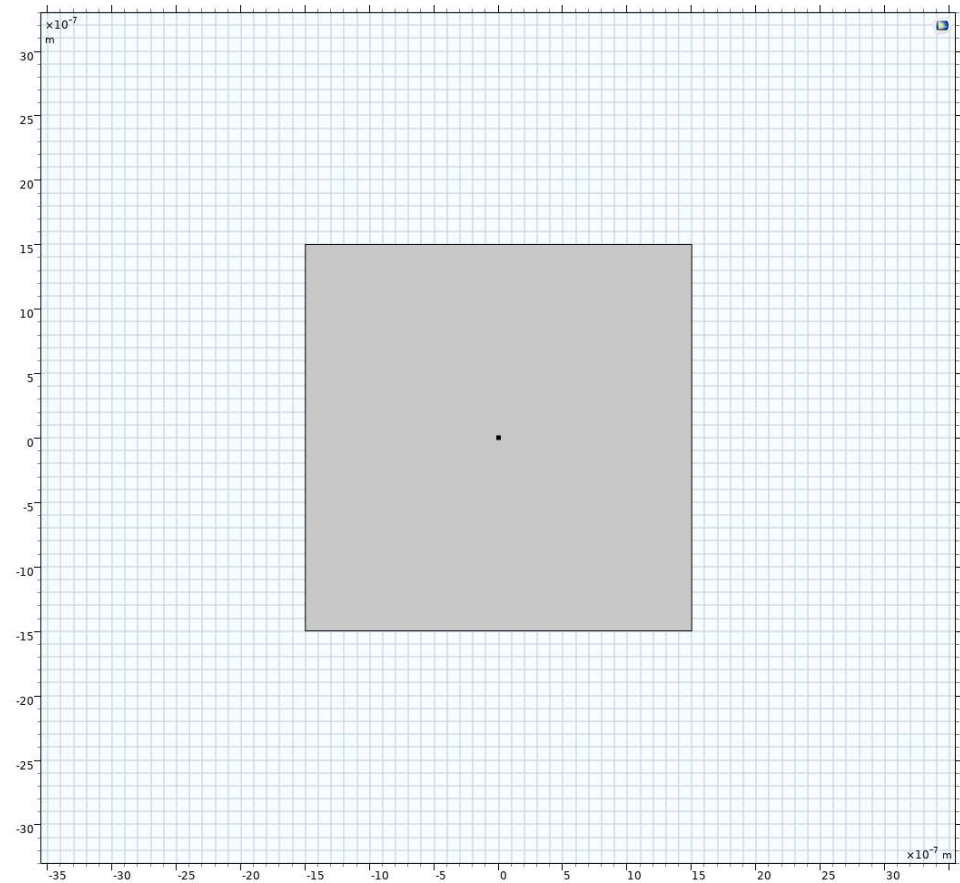


COMSOL: Last Time



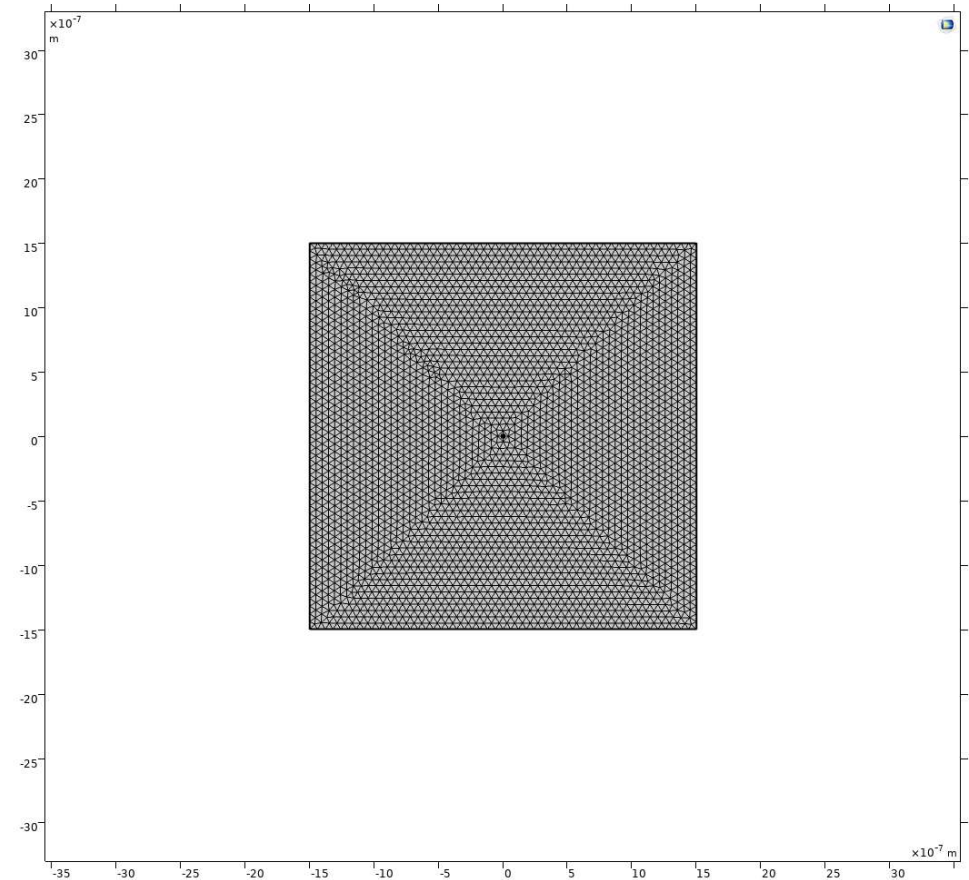
COMSOL: Last Time

- Define simulation domain
- Build geometry

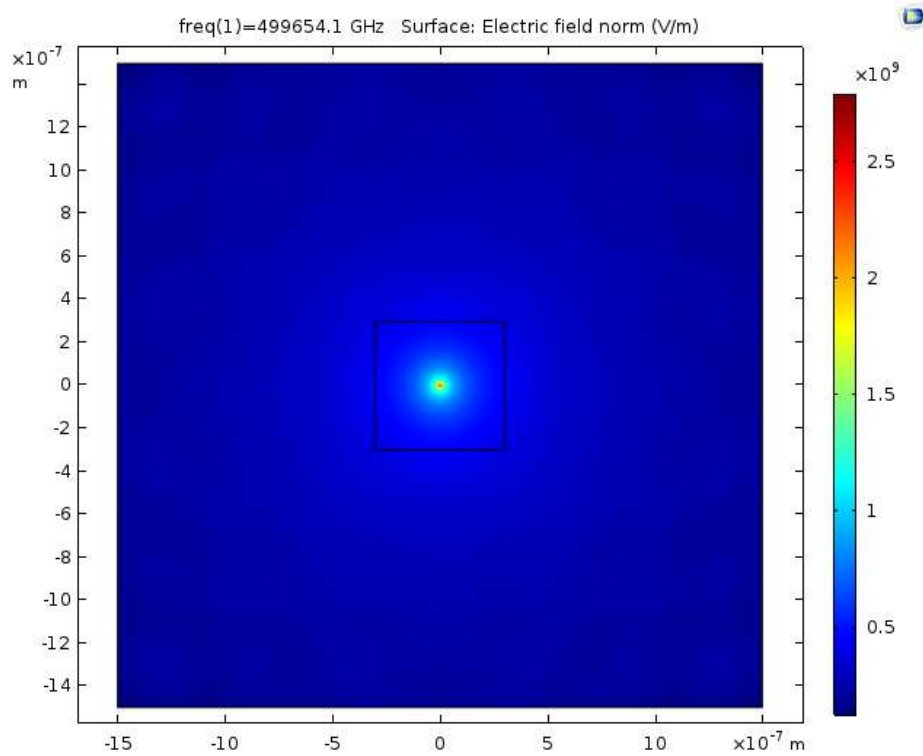


COMSOL: Last Time

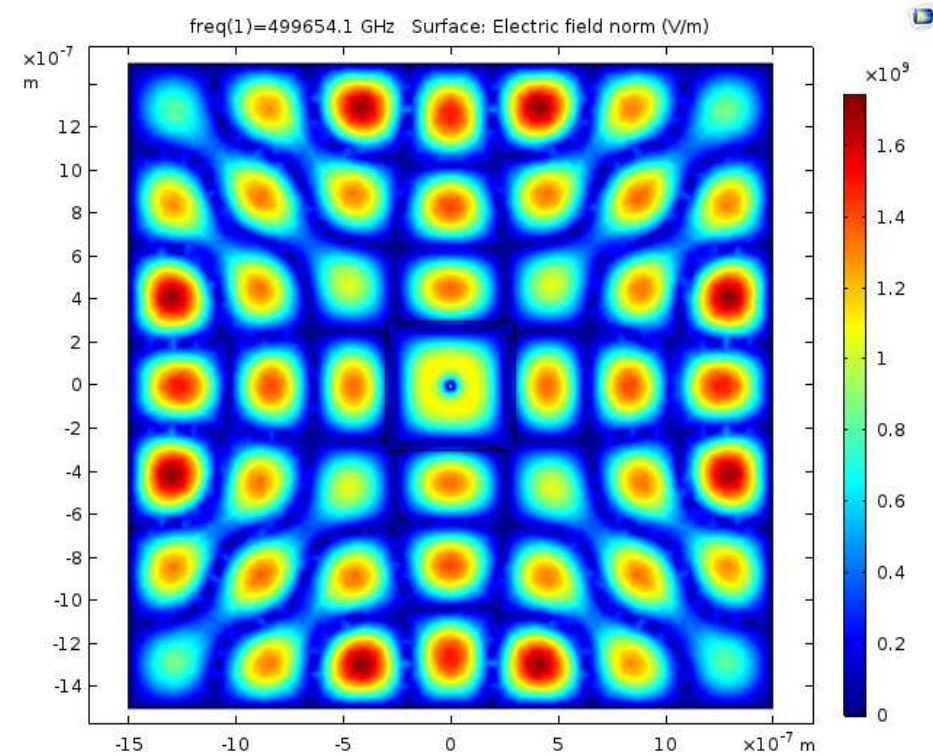
- Discretization of simulation domain
 - Build mesh
- Mesh size determines accuracy of solution
 - Too large mesh $\Rightarrow$ wrong results
- Accuracy vs. simulation time
 - **Today:** Optimization by manual refinement



COMSOL: Last Time



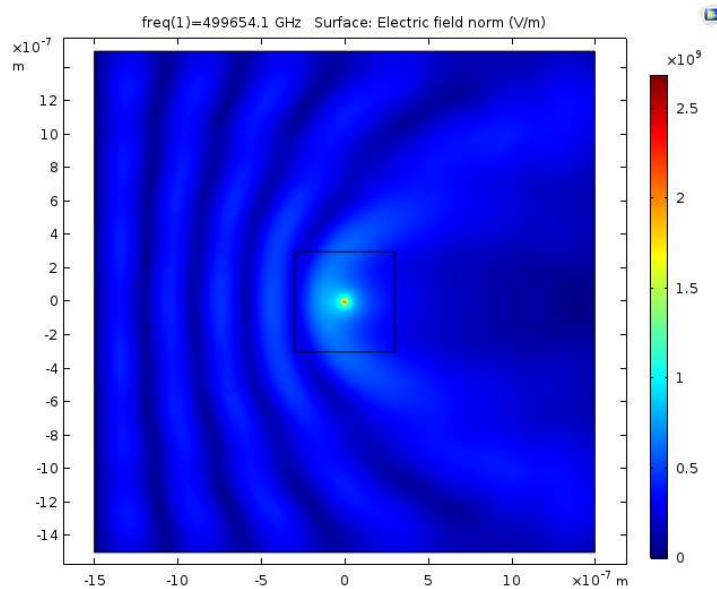
Scattering Boundaries



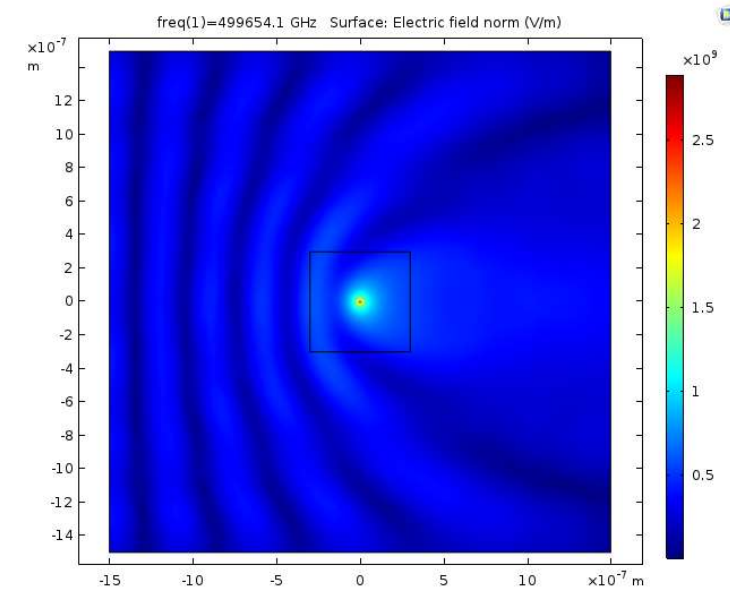
PEC Boundaries

COMSOL: Today

- Mirror effect by using different boundary conditions

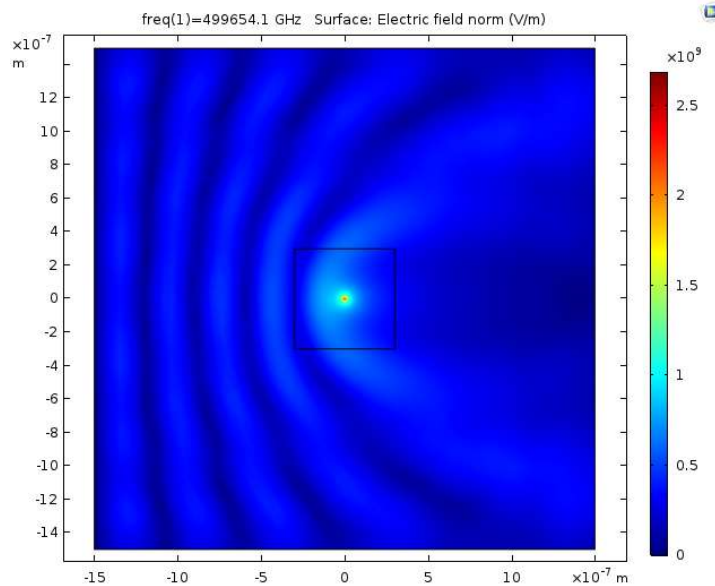


Can you see the difference?
Can you guess the boundary conditions?

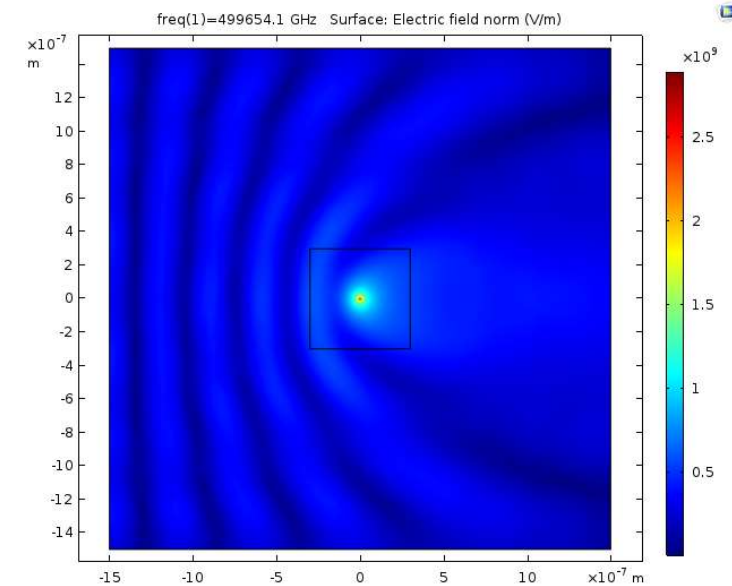
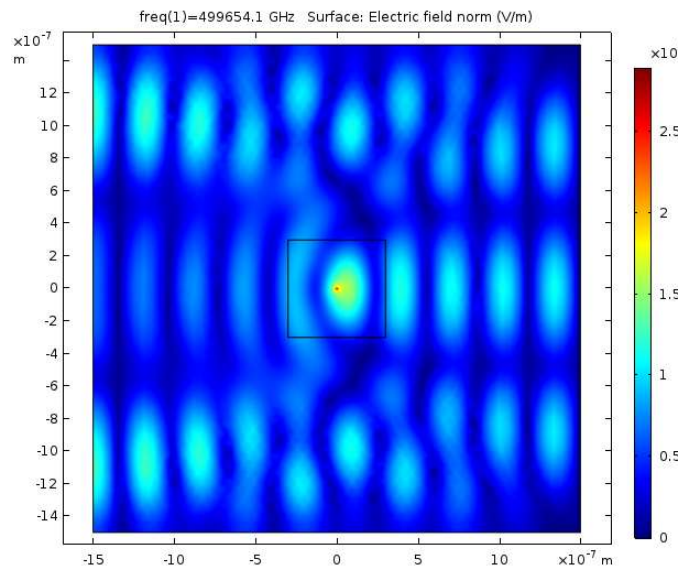


COMSOL: Today

- Mirror effect by using different boundary conditions



Can you see the difference?
Can you guess the boundary conditions?



COMSOL: Today

- Mirror effect by using boundary conditions
- Double Source

